# ANALYSIS OF TREMOR ACTIVITY AT Mt. EREBUS VOLCANO, ANTARCTICA

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Thesis

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This work is dedicated to all people that strength and enlighten my life: my wife Zammya, my children Mario and Carlos, my parents and all my family. Also dedicated to the memory of Diego Viracucha, Victor Hugo Perez, and Alvaro Sanchez, appreciated friends and colleagues, who died in Guagua Pichincha Volcano

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# ABSTRACT

In this study, more than 322 tremor -like signals recorded by the Mount Erebus Volcano Observatory since June 2000 to July 2003 were analyzed. These events occurred in three main periods: 2000-2001, 2002 and 2003, with the second period containing the largest number of tremor episodes and also the largest amplitude one. According to spectral characteristics, these events are classified as harmonic (91%), chaotic (6%) and rapid-fire episodes (3%). Those tremor episodes with small amplitudes and small amplitude ratio between E1S/BOM originate at the outer flanks of the volcano, possibly related to the activity of large and young icebergs. Tremor episodes with large amplitudes have large E1S/BOM amplitude ratios, suggesting that they have a volcanic origin. These events were located using amplitude distribution, semblance, and cross-correlations of envelopes and spectrograms. Their hypocenters were found just beneath the summit plateau or upper flanks of Erebus, several kilometers (3-9 km) deep. Location of episodes with volcanic origin and their apparent disconnection with surface activity, could be related to magmatic recharge processes due to a more mafic and less viscous component than the phonolitic lava observed in the summit crater system. Additional instrumentation (e.g. iceberg-based GPS and seismic recorders) or different location techniques (e.g., array processing) may be useful for locating and discriminating tremor-like signals generated at the outer flanks of Erebus volcano.

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# ANALYSIS OF TREMOR ACTIVITY AT Mt. EREBUS VOLCANO, ANTARCTICA

## **1. INTRODUCTION**

Volcanic tremor is a long duration seismic signal generated inside an active volcano or geothermal field due to internal volcanic processes. Tremor differs from discrete seismic events in having a very emergent initiation, and its largest amplitudes can be located at any part of the episode. One of the more distinctive common characteristics of volcanic tremor is the concentration of seismic energy in narrow frequency bands. When the spacing between these frequency peaks is constant, the signal is called harmonic tremor.

Since the early days of instrumental seismology, tremor episodes have been recorded in active volcanoes (Palmieri recorded tremor signals from Vesuvius in 1856-1873, and Omori recorded Usu eruption' signals in 1911-1912; Davidson, 1927). Nowadays, tremor is one of the most important parameters used in volcano monitoring because it is recognized as the most common short-term precursor of impending eruptions of calderas (Newhall and Dzurisin, 1988) and phreatic eruptions (Barberi et al., 1992). McNutt (1994) documented that 65% of tremor episodes accompany eruptions and 20% precede eruptions in a time frame of minutes to hours. Furthermore, analysis of tremor episodes can bring important information about the type of activity occurring inside the volcano, the location and extension of the magmatic plumbing system, and the

type of fluids that are being transported in it.

Tremor activity has been recorded from 2000 to 2003 at Mt. Erebus volcano by the Mt. Erebus Volcanic Observatory (MEVO) seismic network installed by New Mexico Tech. The objectives of this study are to characterize the tremor activity observed at Mt. Erebus and to examine its implications to the source, and for the structure and dynamics of the volcano. These objectives are intended to be reached based on a description, a classification and a location of the tremor signals. The following activities are addressed here:

Identify tremor episodes in analog and digital seismic records

Obtain parameters of tremor activity and define tremor families

Locate sources of tremor families, and

Discuss models for tremor generation.

In Chapter 2, I present a geological description of Erebus volcano and a review of previous studies of seismicity from Erebus and from icebergs in the Ross Sea area. Chapter 3 contains a description of the seismic network and the instrument responses. An analysis of the temporal evolution of seismic activity and a classification of the different types of tremor episodes is discussed in Chapter 4, and the location of tremor in Chapter 5. Chapter 6 contains a discussion about the different models of tremor generation and their applicability to Erebus episodes. The possibility that some tremor-like signals are generated by the activity of nearby icebergs is discussed on Chapter 7. Finally Chapter 8 contains general conclusions from this research.

# 2. GENERAL CHARACTERISTICS OF Mt. EREBUS VOLCANO

#### 2.1 Regional Geology

Mt. Erebus volcano on Ross Island is the southernmost active volcano in the world, and is located at the southern end of Terror Rift, within the West Antarctica Rift System (Behrendt, 1999). Erebus (3794 m high) is surrounded by the inactive volcanic centers Mt. Terror (3320 m), Mt. Bird (1800 m) and Mt. Terra Nova (2130 m). Kyle et al. (1992) proposed that these volcanoes are an expression of hot-spot magmatism within a rift zone. Seismic studies adjacent to Erebus have shown a crustal thickness of around 18 km beneath McMurdo Sound, seven kilometers thinner than adjacent crust beneath Transantarctic Mountains (McGinnis et al., 1985). The three-fold radial configuration of volcanic centers on Ross Island suggests that the volcanic activity may be controlled by radial fractures in a weak crust (rift zone) above a rising diapir in a hot-spot (Kyle and Cole, 1974, Kyle at al., 1992). Mt. Erebus is an alkaline composite intraplate stratovolcano with predominantly anorthoclase phonolite magma composition. Morphologically, Erebus volcano has a wide base (33 km in diameter) with gentle slopes (13°) that are truncated at an elevation of approximately 3200 m by a summit plateau which hosts a summit Main Crater 600 m wide.

Inside the Main Crater lies the 200 m diameter Inner Crater, which as of 2003, contains a persistent lava lake of phonolitic magma, a small transient lava lake called "Werner's crater" and two small ash vents.

#### 2.2 Description of Erebus activity

Since 1972, observations have described persistent convective activity in the lava lake crater with frequent eruptions ranging from small bubble collapses to small strombolian explosions that threw bombs and ash inside and (rarely) outside the crater. A daily average of 2-6 small strombolian eruptions were counted from 1972 through 1984 (Kyle et al. 1982; Dibble et al., 1984), with explosions at the surface of the lava lake from rising gas slugs up to 10 m in diameter.

In October 1982 activity gradually began to increase and it reached its maximum level between September and December 1984, when strong explosions were heard, seen, and recorded at Scott Base and McMurdo Station, around 40 km away from the crater (Kyle et al., 1994). On 13 September 1984, a large explosion formed an eruption column 4-5 km high that tossed bombs with diameters up to 10 m as far as 1.2 km from the eruptive vent (Kienle et al., 1985, Rowe and Kienle, 1986). The decrease in magnitude and frequency of explosive activity since 1985, is probably related to exhumation of the lava lake and resultant free emission of gas (Kyle et al., 1982; Kyle, 1986).

From August 1999 to July 2001, activity at Erebus again increased with a significant number of strombolian explosions from the lava lake, ash eruptions from the Ash vents, and small lava flows from Werner vents. Changes in eruption intensity, fluctuations in lava lake levels, formation of a new lava pond and formation of an ash vent were observed during the December 2000-January 2001 field season (Wardell,

2002). Wardell (2002) also reported larger and more frequent strombolian eruptions compared to prior years. Tiltmeters on Erebus recorded a change of over 60 µrad, coinciding with a rise in the level of the lava lake which resulted in overflow of the new lava pond and the emplacement of a small lava flow across the floor of the Inner Crater (Kyle et al., 2001). In 2000, a decrease in the As/S ratio measured in gases was consistent with a magma composition richer in sulfur (Wardell, 2002), probably related to a magma injection at depth.

Finally, after a few months of low-level activity, a new period of explosive and seismic activity began in January 2002. It reached its maximum in May 2002 declining afterwards with sporadic and bursts of activity. Eruptive activity has ceased since late Nov. 2002 and continues to be quiescent through to the present day (Oct. 2003).

#### 2.3 Previous seismic studies

The first evidence of seismic activity in the region of Erebus volcano came from seismic records at Scott Base seismic station. Between June 1, 1957 and December 31, 1958, Hatherton (1961) counted in a single station close to McMurdo 76 earthquakes with S-P times of 4 to 6 s, which possibly originated at the volcano.

Systematic observations of the seismicity of Erebus volcano have been reported since December 1980, when a permanent seismic network consisting of four short-period stations with telemetry was installed by the International Mount Erebus Seismic Study (IMESS) project (Dibble et al., 1994). During the field season of 1981-1982, Shibuya et al. (1983) located 162 seismic events. On 8-9 October 1982, more than 700 microearthquakes were recorded with sources located several km beneath the north-western flank. This activity is likely related to a fresh magma injection that preceded the explosive activity which occurred between September 1984 and January 1985 (Rowe, 1988). Between 15-20 explosions a day were recorded at Scott Base station through November, 1984. After March 1985, seismic activity returned to the levels observed between 1980 to 1984.

Dibble et al. (1984) used seismic records from 1975/76 to identify six types of volcanic signals at Erebus: Explosive, B-type, A-type, Harmonic-type, Emergent-harmonic-type and Microearthquake Swarms. Harmonic-type events are characterized by a sinusoidal motion and an extended duration, and Emergent-harmonic-type events have characteristics similar to the Harmonic type but with an extended low-amplitude onset of several seconds.

Knight (1996) carried out a study which provided a description, classification and location of the source of seismic signals recorded digitally by the seismic network of the Mount Erebus Volcano Observatory (MEVO) between November 1994 and June 1996. Long-period, volcano-tectonic, explosive and icequake/tornillo events were studied. Only one tremor episode (January 31, 1995) was reported in this study.

Based on studies using temporary deployment of broadband seismometers at Erebus, very long period (VLP) signals were analyzed by Rowe et al. (2000) and recently by Aster et al. (2003a). VLP signals usually are seen 5 s or more before strombolian

explosions at Inner Crater and contain strong spectral peaks at 8, 11 and 21 s. They are polarized in a radial-vertical plane with somewhat retrograde particle motions. The repeatability of VLP observations indicates a non-destructive or self-reconstructing source mechanism.

#### 2.4 Reports of previous tremor activity

Observations of volcanic tremor in Erebus have been rare in the past. Despite ongoing strombolian activity, Kaminuma (1994) did not report tremor episodes in the 1982-1990 period. Ueki et al. (1984) reported a harmonic tremor episode of 1.1 Hz over a period of one hour in October 8, 1982 during an earthquake swarm, probably related to a dike injection episode beneath Abbott Peak (Kienle et al., 1982; Knight et al., 1996; Rowe, 1998).

A subsequent inspection of analog and digital records from the Erebus seismic network (ABB, FANG and HOO stations) made in this study, revealed an active period of tremor between April to November, 1984, with seven harmonic episodes (April 1, April 10, April 18, May 23, Nov. 14, Nov. 16, and Nov. 18), and one high frequency event (May 16). While harmonic episodes had very short durations (less than 6 min), the high frequency episode lasted about 3 hours. In 1985, four tremor episodes were recorded by the stations E1S, BOM, CON, SIS and HOO, between May 7 and September 21. Events on May 7, June 9 and September 21 have high frequencies and long duration (2-4 hours). The episode recorded on June 10 was of short duration (6 min) and harmonic. No tremor events were identified between 1986 and 1995 despite continued monitoring.

Between 1995 and June 1999, few tremor episodes were recorded. One harmonic tremor episode was recorded at 8 seismic stations on January 31, 1995 (Knight et al., 1996). This event had a maximum amplitude about 5  $\mu$ m/s at E1S and CON (Rowe et al., 2000), and lasted more than 5 min. Its single fundamental frequency decrease slightly from approximately 5 Hz at the beginning of the record to 2 Hz several minutes later (Knight et al., 1996). This signal was seen ~37 km from the volcano at station MCM at McMurdo, suggesting that it was caused by a deep, energetic event (Rowe et al., 2000).

Tremor episodes with a single frequency peak were recorded on April 4, April 5, and August 2, 1998 (Rowe et al., 2000). On May 11, 1998 a tremor episode with 12 harmonics and gliding (frequency-shifting) effect was recorded with a maximum amplitude of 0.6  $\mu$ m/s at E1S (Rowe et al., 2000). Another episode of tremor with similar amplitudes and alternating harmonic and chaotic behavior was recorded on September 2, 1998.

# **3. SEISMIC INSTRUMENTATION**

#### 3.1 Description of the Erebus Seismic Network

Currently, the seismic activity at Mt. Erebus is being recorded with a permanent network of twelve seismic stations, which includes 6 short period and 6 broadband stations. A complete description of seismic and additional instrumentation installed at Erebus is given by Aster et al. (2003b). Stations coordinates and distance to crater are presented in Table 3.1. Station locations are plotted in Figure 3.1.

The six vertical-component short-period instruments (ABB, MAC, CON, HEL, HOO, BOM) are denoted as S.P.Z in Table 3.1. Two other short-period stations, SIS (short-period, 3 components) and ICE (short-period vertical) were marginally operating between January and March, 2001.

There are five permanent broadband stations on the volcano (with code B.B.3C in Table 3.1). E1S station was installed in December 2000 (Aster et al., 2003a; url: www.ees.nmt.edu/Geop/mevo/seismic/seismicity). Stations NKB, LEH, CON and HOO were installed in January 2003 as part of the Integrated Surveillance Instrumentation package (ISI) that upgraded the capabilities of the monitoring instrumentation at Erebus. CON and HOO have both short period and broadband stations with the same name. An additional broadband station is located 38 km from the volcano at Scott Base (SBA) and belongs to the Global Seismic Network (GSN).

STATION	TYPE	LAT. S	LONG. E	ALT. (m)	DIST (km)
MAC	S.P.Z	77.53247	167.24639	3332	2.07
CON	S.P.Z	77.53463	167.08515	3453	2.09
HEL	S.P.Z	77.50538	167.17394	3362	2.41
HOO	S.P.Z	77.53159	166.93236	2121	5.62
BOM	S.P.Z	77.50894	167.44018	2014	6.95
ABB	S.P.Z	77.45699	166.90908	1789	9.96
E1S	B.B.3C	77.53053	167.14070	3708	0.69
NKB	B.B.3C	77.52200	167.14710	3501	0.70
LEH	B.B.3C	77.51070	167.14110	3295	1.90
CON	B.B.3C	77.53463	167.08515	3453	2.09
НОО	B.B.3C	77.53159	166.93236	2121	5.62
SBA	B.B.3C	77.84890	166.75740	20	37.96

Table 3.1 Location of permanent short period ( $\underline{S.P.Z}$ ) and broadband (B.B.3C) seismic stations at Mt. Erebus volcano with distances between stations and the inner crater.

Several problems, such as low temperatures, strong winds, and the accumulation of hoarfrost affected the normal operation of seismic stations, especially during the austral winter, resulting in power shortages, disorientation of the antennas and damage to electronic components. For these reasons, only few stations have been operating through the extreme winter season at Erebus. Table 3.2 summarizes the operating times of stations in the Erebus Network.

STAT	ABB	BOM	CON	HEL	HOO	MAC	E1S.B	CON.B	HOO.B	LEH.B	NKB.B	SBA.B
Ja00												
Fe00												
Mr00												
Ap00												
Ma00												
Jn00												
J100												
Au00												
Se00												
Oc00												
No00												
De00												
Ja01												
Fe01												
Mr01												
Ap01												
Ma01												
Jn01												
J101												
Au01												
Se01												
Oc01												
No01												
De01												
Ja02												
Fe02												
Mr02												
Ap02												
Ma02												
Jn02												
J102												
Au02												
Se02												
Oc02												
No02												
De02												
Ja03												
Fe03												
Ma03												
Ap03												
My03												
Jn03												

Table 3.2 Operation of seismic stations (Jan. 00 – June 03)

Other seismic stations have recorded tremor episodes from Erebus volcano, such as the broadband seismic station VNDA, located in the Dry Valleys, near the lake Vanda. Broadband seismometers were deployed temporarily during the TAMSEIS experiment (WUSTL Seismology Group, 2003). For this experiment two linear arrays of stations crossed the Transantarctic Mountains to image details of the crust and upper mantle structure across the East-West Antarctic boundary.



Fig. 3.1 Seismic network at Erebus volcano. Short period stations are shown as small red squares and broadband stations as larger red squares (including SBA station). One station from TAMSEIS experiment is shown as a blue square. VNDA and the other TAMSEIS stations are located outside the area shown by the map.

#### 3.2 Additional instrumentation

Seismic observations at Erebus volcano are complemented by visual, infrasound, infrared, geodetic, geochemical and environmental observations providing valuable data for a better description of Erebus activity. Most of the additional instrumentation operates intermittently due to power availability. It includes:

North crater rim: A video camera located at 400 m from the lava lake providing GPS time-stamped observations of the vents within the Erebus crater.

E1S: The broadband seismic station at E1S is complemented with a biaxial (radial and tangential) tiltmeter and dual-frequency GPS receiver for geodetic monitoring, two infrasound microphones for detecting the strong degassing and explosive activity, and finally sensors that monitor temperature, wind speed and wind direction.

NKB: This station was upgraded with two infrared sensors, an infrasound microphone, geodetic instruments (GPS, radial and tangential tilt) and a temperature sensor.

LEH: In addition to the broadband station, a GPS receiver, a tiltmeter and sensors to monitor temperature, wind speed, wind direction, pressure, and humidity were installed.

CON: Short period and broadband seismic instruments are complemented with

GPS and environmental sensors: temperature, wind speed and direction sensors.

HOO: Short period and broadband seismic instruments are complemented with temperature, wind speed and direction sensors.

## 3.3 Determination of in-situ response of seismic stations

We investigated the in-situ response of the seismic network using teleseismic signals. This was done because the older short-period stations may differ significantly from their specifications due to aging, and because there may be strong site effects at some stations in the short period band. Seismic signals from nine teleseismic events listed in Table 3.3 were analyzed in order to determine the gain factors of the short period stations. These teleseismic events are recorded both by the short period and broadband stations and represent an approximately plane-wave excitation of the network from a distant source. Records for Scott Base station (SBA) were provided by the Data Management Center of IRIS. This set of teleseismic events was selected because they were recorded at all short-period stations without clipping. Figure 3.2 shows seismic signals of the teleseismic event recorded on March 25, 2003 without correction for magnification.

A matlab code TELECALIB.M written by R. Aster was used to get amplitude ratios for the seismic stations for each teleseismic event. This code takes a portion of the seismogram containing the teleseismic event between two signal-marks, T1 and T2, filters the signals into the 0.8 to 5.0 Hz band, calculates the Hilbert Transform, and shifts



and scales the envelopes in order to achieve the best match (Figure 3.3).

Fig. 3.2 Teleseismic event recorded on March 25, 2003 at all seismic stations of Erebus network. Vertical scale is given in counts and none of the traces is clipped. A 0.8 to 5.0 Hz Butterworth bandpass filter was applied to all signals.



Fig. 3.3 Envelopes of the March 25, 2003 event, which were calculated using the Hilbert transform. All seismic traces have been aligned using time lags found with cross-correlation analysis. Amplitude ratios are calculated using these signal envelopes.

Once all signals are aligned, amplitude factors  $a_{ij}$  of the signal envelopes are computed for each of the *i*<sub>th</sub> station and *j*<sub>th</sub> teleseismic event (Table 3.4). Sets of normalized amplitude factors  $a'_i$  were computed using the 2-norm of the  $a_i$  factors corresponding to this event. This calculation was repeated for all *j*<sub>th</sub> events.

$$(a'_{i})_{j} = (a_{i})_{j} / ||(a_{i})_{j}||$$
(3.1)

The amplification factor for each *i*th station was calculated with the median value of all corresponding factors.

$$af_i = median(a'_1)_j \tag{3.2}$$

An average of the amplification factors and gains for the broadband stations with well known gain constants (E1S, CON, NKB, LEH and HOO) were used as reference  $af_{ref}$ . Then gain factors for each short period station were calculated using the following expression:

$$Gain_{i} = af_{ref} * Gain_{ref} / af_{i}$$
(3.3)

Considering the theoretical values of gain constant of short period stations and these empirical gains obtained with Eq. 3.3, a gain calibration constant was found for each seismic station. Gain factor and calibration constant for each station are given in Table 3.5. The amplitude of ground motion in  $\mu$ m/s for each seismic station can be obtained using the product of the signal amplitude (in counts) with the corresponding gain factor ( $\mu$ m/s/count).

EVENT DATE	HOUR	LAT	LONG	DEPTH (km)	Mw	Epicentral region
2003-01-271	17:56:26	46.048 S	35.057 E	10	6.5	Prince Edward Is.
2003-02-122	22:34:03	1.4 S	142.5 E	33	NR	New Guinea
2003-02-10 <sup>2</sup>	04:49:30	6.1 S	149.8 E	33	6.3	New Britain Is.
2003-03-10 <sup>2</sup>	02:09:32	1.9 N	127.0 E	93	6.4	Molucca
2003-03-111	07:27:33	4.694 S	153.24 E	40	6.8	New Guinea
2003-03-143	02:55:00	62.10 S	161.73 E	33	5.9	Balleny Is.
2003-03-251	02:53:25	8.294 S	120.743 E	33	6.5	Flores Is.

Table 3.3 List of teleseismic events used for determination of amplitude factors.

 <sup>1</sup> Data from NEIC: Significant Earthquake List, <u>http://www.neic.cr.usgs.gov/neis/eqlist/sig\_2003</u>
 <sup>2</sup> Data from BGR: Local and Teleseismic Bulletins <u>http://www.szgrf.bgr.de/bulletins</u>
 <sup>3</sup> Data from IRIS: WilberII <u>http://www.iris.edu/cgi-bin/wilberII</u>

Station/TS	ts30127	ts30210	ts30212	ts30310	ts30311	ts30314	ts30325
ABB.EHZ	1.994	1.933	1.989	2.427	2.578	2.487	2.608
BOM.EHZ	3.555	3.423	3.508	3.620	3.831	4.171	4.407
CON.EHZ	0.976	0.834	0.971	0.890	0.944	1.018	0.859
HEL.EHZ	1.129	2.191	1.507	1.389	1.808	1.391	1.502
HOO.EHZ	2.835	3.516	3.742	3.586	3.289	3.285	3.565
MAC.EHZ	1.024	0.865	0.933	1.110	1.056	0.953	1.111
E1S.BHZ	0.487	0.985	0.812	0.667	0.681	0.639	0.641
CON.BHZ	0.608	0.934	0.889	0.619	0.616	0.736	0.571
HOO.BHZ	0.650	0.993	1.029	0.858	0.801	0.960	0.889
LEH.BHZ	0.479	1.007	0.842	0.603	0.676	0.982	0.594
NKB.BHZ	0.416	0.694	0.645	0.553	0.633	0.575	0.798
SBA.BHZ	3.506	5.739	5.293	3.624	4.560	7.676	3.921

Table 3.4 List of amplitude factors  $a_{ij}$  obtained from teleseismic events

Table 3.5 Gain factors  $Gain_i$  and calibration constants  $af_i$ 

Station	Theoretical Gain 10⁴(um/s/count)	Empirical Gain 10 <sup>-4</sup> (um/s/count)	Calibration constant
ABB.EHZ	1.2589	2.6895	2.1365
BOM.EHZ	1.2589	1.6864	1.3396
CON.EHZ	10.0708	6.9493	0.6901
HEL .EHZ	10.0708	4.3235	0.4293
HOO.EHZ	2.5177	1.8917	0.7513
MAC.EHZ	5.0354	6.1173	1.2149
SBA.BHZ	1.1936	1.4200	1.1896
E1S.BHZ	0.0000	10.8906	1.0000
CON.BHZ	0.0000	8.0176	1.0000
HOO.BHZ	0.0000	7.9912	1.0000
LEH.BHZ	0.0000	7.9687	1.0000
NKB.BHZ	10.8781	10.8781	1.0000

## 3.4 Validation of empirical gain factors

Ground motion amplitude ratios for 36 tremor episodes were evaluated for simultaneous recordings of the short period seismometers at CON.EHZ and HOO.EHZ and the corresponding broad band components (CON.BHZ and HOO.BHZ). All these signals were filtered in the band from 0.8 to 5.0 Hz to remove microseisms and high frequency contamination and so that the data samples would be homogeneous. Considering that these events were recorded at the same locations, signal differences should be attributable only to instrument response of each seismometer. Assuming that the response function for the broad band station is exact, it was possible to calculate the instrumental response of short period station in the range of 0.8 to 5.0 Hz. Figure 3.4 shows amplitude parameters for recordings from the stations CON and HOO with broadband and short period seismometers.

Small residuals between short-period and broad-band stations (CON and HOO) validate the gain factors found in this chapter. In further applications, these empirical gain factors will be used.



Fig. 3.4 Upper part: *rms* amplitudes of 36 tremor episodes recorded simultaneously on broadband and short period seismometers at stations CON and HOO (filtered from 0.8 to 5.0 Hz). Residuals of absolute amplitudes between short period and broadband stations are plotted in lower part of the plot.

## 3.5 Seismic velocity models for Erebus volcano

Several efforts have been made to determine a general velocity structure for Mt. Erebus and the surrounding area (Dibble et al., 1994). The following is a summary of the most significant of these attempts (some velocity determinations from the early 80's have been omitted): a) Using teleseismic events:

Dibble et al. (1984) found an average velocity of  $4.5 \pm 1.3$  km/s for the volcano using variations in the arrival times versus station altitude for six selected teleseismic events with nearly vertical incidence angles.

b) Refraction experiments:

Dibble et al. (1994) using a 330 m-long refraction experiment conducted in 1989 between the Upper Hut and NKB stations, found a shallow velocity of  $3.0 \pm 0.3$  km/s for this area. A larger survey carried out along a 1.4 km line (from crater to CON station) found a permafrost layer 90 m thick with a velocity range of 1.0 to 1.9 km/s was overlying a reflector with velocities up to 4.0 km/s.

c) Arrival times of explosion events:

Dibble et al. (1988) determined a mean  $v_p$ =4.07 km/s using a stack of nine strong explosion events from December 1989. They were recorded on six stations at distances from 0.7 to 10.1 km from the crater. Inside a radius of 0.7 km around the magmatic conduit, they also found a low velocity zone of scoria with  $v_p$ =1.5 km/s. Outside this area, the p-wave velocity in the surface permafrost is about 3 km/s. This is underlain to average depths of about 360 m by regions with low velocities of 1.0 to 2.4 km/s. Below this level, velocities of 4.1 to 4.3 km/s are observed between 1 and at least 10.1 km distance from the explosions. 5.5 km below the crater, the Mt. Erebus edifice is thought to be underlain by a low velocity layer of sediments and by an igneous basement with a velocity of 6.5 km/s (Dibble et al., 1994).

Using a set of 28 explosions, Rowe (1998) found that the minimum residuals for those events were obtained using velocities of 3.44 to 3.54 km/s.

Johnson et al. (2003) estimated an apparent p-wave velocity of  $3.3 \pm 0.3$  km/s for the northern summit plateau region using the first arrivals of explosion signals.

d) Induced blasts

Using the arrival times for nine induced blasts recorded at distances between 3.95 and 13.5 km, Dibble et al. (1994) found a value of 4.3 km/s for a horizontal layer between 0.58 km to 6.1 km depth. Rowe (1988) found a velocity gradient with its minimum at the volcano summit ( $v_p = 3.55$  km/s) and a maximum of 4.6 km/s at 7 km depth beneath the summit.

In this study, a homogeneous and isotropic half space with a velocity of 4.07 km/s (Dibble et al., 1988) will be used, considering that this velocity was obtained through a large array and covers the interest range of depth for tremor episodes (from summit to 5.5 km deep).

# 4. DESCRIPTION OF TREMOR ACTIVITY

### 4.1 Data presentation

A systematic search for tremor episodes in the digital and analog records from the Erebus seismic network found 323 tremor events between 03/20/1999 and 07/26/2003. For each tremor episode, onset time, end time, maximum velocity ( $\mu$ m/s) and the root-mean-square (*rms*) of velocities in each seismic station are stored in a database, as well as the fundamental frequency (*fo*) and number of overtones (*n*). Maximum ground motion displacements ( $\mu$ m), and reduced displacements (*RD*) in cm<sup>2</sup> for each station were also computed. Durations of events and releases of energy in arbitrary units have also been obtained from previous parameters. All this information is recorded in a database that contains files /raid/data/Erebus/Tremor/DR-harm3.SDC and /raid/data/Erebus/Tremor/FRQ-harm2.SDC.

A matlab code pretrem2.m was used to convert velocity series into displacements and compute the *rms* and maximum velocity. Reduced displacements for body waves  $(RD_{bw})$  were calculated using the following expression adapted from Aki and Koyanagi (1981):

$$RD_{bw} = 10 \, u_{max} \, r / 2 \, \sqrt{2} \tag{4.1}$$

 $u_{max}$  is the largest displacement (in  $\mu$ m) after correction for the instrument magnification,

Seismic energy released by tremor episodes was calculated as

$$E_i = \kappa[(1/n) \sum v_j^2] \Delta t_i, \qquad (4.2)$$

where  $v_j$  is the *j*<sub>th</sub> value of ground motion velocity in µm/s, *n* is the length of data series,  $\Delta t_i$  is the episode duration and  $\kappa$  is an arbitrary factor.  $E_i$  is a relative energy for *i*<sub>th</sub> episode. The monthly release of energy was computed as the sum of the energy released by individual tremor episodes.

Table 4.1 gives a small sample of the main signal characteristics stored in the database. It contains nine large amplitude harmonic events or harmonic events with a large number of overtones, two rapid-fire and, and one chaotic event.

Date	Onset	End	Num.	$u_{max}$	RD	E (arb.	Fo	Num.	Туре
m/d/y	time	time	stations	(um/s)	( <i>cm</i> <sup>2</sup> )	units)	(Hz)	Harm.	
2/3/01	00:31	02:52	6	48.5	52.4	30033	1.25	6	Harm
2/23/01	12:14	12:29	6	35	52.9	31928	2.1	14	Harm
6/26/01	23:15	00:27	5	23.3	54.8	14781	1.3	30	Harm
5/21/02	06:08	07:45	3	97.8	92.6	621286	1.8	10	Harm
7/17/02	10:05	10:37	1	1.96	1.5	111	1.05	52	Harm
1/30/03	10:35	11:57	10	3	4.4	1133	0.24	30	Harm
2/2/03	15:10	15:50	11	4.9	3.5	166	1.3	5	Harm
4/10/03	00:15	01:30	11	64.7	55.3	7090	0.6	1	Harm
4/12/03	06:48	08:08	11	8.2	9.7	2171	0.55	5	Harm
3/27/03	05:35	06:26	11	10.5	8.5	851	-	-	Chao
1/18/03	10:55	11:23	11	7.3	6.4	740	1.5	-	RF
2/1/03	11:00	11:39	11	12.9	12.2	2043	1.5	-	RF

Table 4.1 Data base of selected tremor events containing main parameters of tremor episodes (date (month/day/year), onset time (hh:mm), end time (hh:mm), number of stations, maximum ground motion amplitude ( $u_{max}$ ), reduced displacement (*RD* in  $cm^2$ ), relative released energy (*E*), fundamental frequency ( $f_o$  in  $H_z$ ), number of harmonics or overtones (n) and the type of tremor (Harm= harmonic, Chao= chaotic, RF= rapid-fire), for twelve of the tremor events.

### 4.2 Time distribution of recent tremor activity

Tremor activity started to become conspicuous in June 2000, although sporadic episodes were recorded between April 1999 and April 2000. Based on the distribution of the number of tremor episodes (Fig. 4.1), three apparent periods can be distinguished: June 2000- October 2001, January - December 2002, and January - July 2003.

## 4.2.1 First period of activity (June 2000 - October 2001)

The first period contains 68 tremor episodes with a maximum ground movement of 48.6 um/s at E1S (52.4 cm<sup>2</sup>), the closest station (02/03/01). The monthly average of
tremor episodes during this period is 4.0. February 2001 has 18 tremor episodes and also the largest energy release in the period. From June 2000 to January 2001, tremor episodes typically have short durations (less than 10 min). However, after February 2001 there is a marked increase in duration of tremor episodes, reaching a maximum of 177 min. The median of the duration during this period is 18 min (Fig. 4.2).



Fig. 4.1 Monthly number of tremor episodes recorded on Erebus volcano (in bars) in the period Jan. 1984 -Dec. 1985 and Jan. 1995 -Oct. 2003. No minimum magnitude criteria was established to consider them. The red dashed line shows the tremor relative energy releases. Some discrepancies between the number of events and energy release are explained as months with large amount of tremor with small amplitudes, for instance between Jun.-Dec. 2000, Jul. 2001 or Jul.- Dec. 2002. The monthly number of explosions (blue line) is scaled on the right side. Data for Oct-Dec. 1984 was obtained from digital records provided by R. Dibble. 1984-1985 period was completed with the number of local shocks counted by Kaminuma (1984), using an explosions/shocks ratio found in Oct.-Dec. 1984 period. Information for 1995-1996 period was taken from Knight (1996). First (1), second (2) and third (3) periods are bounded by vertical dashed lines. On a long-term scale, there is a roughly inverse relationship between explosion occurrence and the number and energy release by tremor episodes.

4.2.2 Second period of activity (January 2002 - December 2002)

The second period, with 160 tremor episodes, began on January 2002 and lasted until December 2002. During this period, the monthly average of episodes was 13.0. The largest number occurred in June 2002 (50 episodes). Compared with the first period, there is a large increase of duration of tremor episodes (Fig. 4.2). The median of the tremor duration is 50 min, with 21 events lasting more than 2 hours and one lasting 5 hours (Sept. 19, 2002). The increase in the number and the durations of episodes results in an increase in the energy release. The largest energy release was during May, when 45 tremor episodes were recorded. The largest tremor amplitude reached 97.8  $\mu$ m/s at E1S (DR=92.6 cm<sup>2</sup>) on May 21, 2002.

4.2.3 Third period of activity (January2003 - July 2003)

The monthly average number of tremor episodes during the last period of activity is 13.4. The largest episode occurred on April 10, with an amplitude reaching  $64.7 \,\mu$ m/s at E1S. April and June 2003 had the largest number of tremor episodes (19) in this period. The duration of tremor episodes has the same distribution observed during the second period although with smaller values: seven episodes had durations longer than 2 hours (Fig. 4.2), and an episode on March 28, 2003 had the longest duration of 221 min. The largest amount of energy was released during January 2003.



Fig. 4.2 Duration of tremor episodes at Erebus volcano for the three periods of activity and a summary which contains the duration from January 2000 to June 2003.

## 4.3 Frequency distribution of tremor episodes

The data file /raid/data/Erebus/Tremor/FREQ-harm2.SDC contains information about the fundamental frequency  $f_o$  (the lowest frequency associated with a harmonic), number of harmonics (*n*), spacing between harmonics at the period of the largest amplitudes and frequency associated with the maximum amplitude, also called peak frequency). Spectra were calculated using the FFT algorithm from Passcal Quick Look PQL. Linear scale on frequency axes and logarithmic scale on amplitudes of signal spectra were useful for recognizing harmonics (equally frequency-spaced spectral peaks). In special cases, power spectra were calculated using the multitaper pmtm code in Matlab to enhance the spectral peaks.

No evidence of very long period components were found in the tremor episodes at Erebus volcano, as such has been observed at Popocatepetl volcano (Arciniega-Ceballos et al., 2003).

4.3.1 First period of tremor activity (Jun. 2000 to Dec. 2001)

During the first period, fundamental frequencies are distributed between 0.35 and 4.0 Hz, with a median value of 1.25 Hz and standard deviation of 0.81 Hz (Fig. 4.3). Most of the fundamental frequencies are in the band between 0.5 and 1.5 Hz, especially due to the frequencies associated to tremor swarms of February and July 2001. There are small peaks around 2.2 Hz and 3.5 Hz, present from June 2000 up to February 2001. Most of the events have fewer than 8 overtones, with a median value of 3 overtones per event with a standard deviation of 4.6 (See Fig. 4.4). Only three episodes do not have harmonics and one tremor episode, occurring on June 26 at 23:40, exhibited 30 harmonics.

4.3.2 Second period of tremor activity (Jan. to Dec. 2002)

As shown in Fig. 4.3, the second period exhibits a small decrease in the median of  $f_0$  (1.05 Hz ) with also a smaller standard deviation (0.69 Hz ). Most of the events (83%) have frequencies in the range 0.5 to 1.5 Hz. Most of the episodes of the big tremor swarm of May-June 2002 have fundamental frequencies in this range. Seven episodes have frequencies smaller than 0.5 Hz in October 2002. Nine events during the May swarm present frequencies larger than 2.5 Hz (Fig. 4.3). Most of the tremor episodes have fewer than 9 overtones with few exceptions, with the largest one, occurring on July 17, 2002, having 51 overtones (Fig. 4.4). The high number of overtones is related to the presence of sub-harmonics in between of each pair of principal spectral peaks. Occurrence of these multi-harmonics appears to be unrelated to signal to noise ratio or amplitude of the signal.

#### 4.3.3.- Third period of tremor activity (Jan. 2003 to present)

The third period shows a clear decrease in the median value of the fundamental frequency distribution (0.80 Hz) with a standard deviation of 1.24 Hz (Fig. 4.3). Frequencies are distributed between 0.24 to 7.7 Hz, with 5 episodes around 4.0 Hz. As was seen in previous periods, tremor episodes commonly have fewer than 9 harmonics (Fig. 4.4). The median of the number of overtones is 2.0 with a standard deviation of 3.9. One tremor episode on Jan. 30, 2003 at 10:35 had 30 overtones and it is also related to a period-doubling effect.



Fig. 4.3 Distribution of fundamental frequencies (frequencies associated with larger amplitudes on tremor episodes). Upper panels and lower-left panel shows the frequency distribution during the three activity periods. Data in lower-right panel considers the total number of events.



Fig. 4.4 Number of overtones observed in tremor episodes of Erebus volcano. Upper-left panel corresponds to the first period of activity (June 2000 to October 2001). Upper-right panel shows distribution of number of harmonics during the second period (January to December 2002). Lower-right panel corresponds to the third activity period (January to June 2003). Lower-right panel summarizes the distribution of the number of overtones throughout the entire activity period (June 2000-June 2003).

## 4.4 General classification of tremor episodes

An empirical classification of tremor episodes recorded at Erebus has been carried out based on some features of waveforms or spectral characteristics (number of overtones, gliding effect, etc.). Three types of tremor have been recognized: harmonic, chaotic, and rapid-fire (Table 4.2, Figure 4.5). We have to consider also the fact that even a single tremor episode could share two types of oscillation. Harmonic episodes tend to have a chaotic part in 42% of the cases. All of these cases have been counted only as harmonic episodes. Rapid-fire tremors are usually preceded by chaotic events. These episodes have been counted only as rapid-fire episodes.

Tremor type	Characteristics	
Harmonic	Energy seen in one spectral peak	
	(fundamental frequency $f_o$ ). Generally with	
	one or more overtones located at exact	
	multiples of $f_o$ (Hellweg, 2000).	
Rapid fire	Sequence of very similar, but independent,	
	impulsive events (Hellweg, 2000). The	
	term spasmodic tremor refers a sequence of	
	pulses of high frequency, usually 5-0 Hz or	
	more (McNutt, 1994), often associated	
	with fractures.	
Chaotic	Broad spectrum without overtones.	

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Table 4.2	Types	of tremor	episodes
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Fig. 4.5 Distribution of types of tremor episodes on Erebus volcano during the period 1999-2003.

## 4.4.1 Harmonic Tremor

Harmonic tremor episodes (Fig. 4.6) are characterized by spectra with at least one distinctive spectral peak. Harmonics are all distributed at constant frequency spacing. Fundamental frequency,  $f_{0}$  is the spectral peak located at the lowest frequency, which usually corresponds to the highest amplitude peak. Monochromatic tremors have most of the energy concentrated on one small frequency band. Spectra of these episodes have a single narrow peak with no overtones or very low amplitude.



Fig 4.6 Harmonic tremor at Erebus volcano. The fundamental frequency is almost constant along this episode at 2.0 Hz. At least six overtones are recognized keeping the same frequency interval. At the beginning of the episode, a higher frequency monochromatic trigger event is observed with a duration of 3 min.

Some harmonic tremor episodes exhibit a series of special characteristics such as gliding, frequency shifts, period doubling and trigger phases.

4.4.1.1 Gliding.- Changes in the value of  $f_0$  are commonly observed in tremor episodes. These variations are reflected proportionately in the frequencies of the overtones  $f_n$ . These frequency changes occur in all stations at the same time, indicating that such changes must be generated at the source, as could be expected for linear wave propagation. Around 11% of the tremor episodes recorded on Erebus volcano have a general upward gliding (Fig. 4.7), and 39% show a downward trend (Fig. 4.8). Near half of the harmonic tremors (49%) show stable spectral peaks frequencies or small variations of the fundamental frequency  $f_0$  and  $f_n$  overtones along the episode, as seen in Figure 4.6.



Fig. 4.7 Upward gliding observed after time 2200 s on the tremor episode on Feb. 9, 2001 from 13:24 to 14:10 by the vertical component of E1S broad-band seismic station. In 8 min, the fundamental frequency  $f_o$  changes from 1.9 Hz to 5 Hz (more than 160% of variation with respect to initial value of  $f_o$ ). An icequake is recorded at time 2150 s with impulsive onset, short duration and broad spectral content.



Fig. 4.8 Harmonic tremor of Erebus volcano showing downward gliding. Upper panel shows the seismic signal recorded on Feb. 2, 2001 since 05:41 by the vertical component of E1S station (0.7 km from crater). Fundamental frequency decreases from 1.8 Hz to 0.7 Hz where it merges in a chaotic tremor. All overtones maintain the same proportional pattern.

4.4.1.2 Frequency shifts.- Sharp frequency shifts are also observed in fundamental frequency of tremor episodes recorded in different stations. A frequency shift from 3 Hz to 4 Hz is observed on E1S record of February 9, 2001 at time 2700 s (Fig. 4.7). A rapid change in spectral frequencies is denoting drastic changes in the properties of the harmonic tremor source. Spectra of time series containing frequency shifts may produce apparent "multiple" oscillation modes.

4.4.1.3 Period doubling.- In few cases, spectra of tremor episodes at Erebus show the presence of short-duration secondary spectral peaks between two larger spectral peaks observed in the spectrum for longer time (Fig. 4.8). Julian (2000) explained the presence of subharmonic frequencies in non-linear constricted flow oscillations as period doubling, where at a certain critical value of the control parameter a new frequency appears which is half of the previous repetition frequency. Spectra of seismic signals with doubling period effects show an increase in the number of overtones and an apparent decrease the value of  $f_0$ .



Fig. 4.9 Upper panel: 1 min-window signal of tremor episode recorded on July 17, 2002. A band-pass 0.3 to 15 Hz filter was applied. Lower panel shows a power spectra density computed using *pmtm.m* code. The fundamental frequency is located at 1.05 Hz, has the largest amplitude. Harmonic spectral peaks are located frequencies  $nf_o$ . Between main harmonics, two low-amplitude pulses are clearly seen. They are equally spaced at 0.35 Hz.

4.4.1.4 Trigger phase.- Some tremor episodes, either harmonic or chaotic, exhibit a short-duration trigger phase. This phase has usually small amplitudes and higher frequencies values compared to the fundamental frequency of the main episode. In the February 23, 2001 episode, a trigger phase with a frequency around 9 Hz lasts 160 s (Fig. 4.6). The tremor episode recorded on February 2, 2001 has a trigger phase at 4.6 Hz with one overtone at 9.2 Hz (Fig. 4.8).

4.4.2.- Chaotic Tremor

Chaotic tremor episodes are characterized by broad spectra without a predominant frequency peak. Usually tremor episodes with chaotic spectral patterns show a spindle-shaped waveform. An example of chaotic tremor is shown in figure 4.10.



Fig. 4.10 Chaotic tremor episode recorded on March 27, 2003 at the vertical components of broad-band stations E1S and CON. No clear spectral peaks are observed and seismic energy is distributed between 1 and 8 Hz.

#### 4.4.3.- Rapid-Fire tremor

Characterized by a sequence of pulses or shocks with similar size and duration occurring in a short period of time, usually with overlapped codas. These signals usually do not have high frequencies ( $\geq 10$  Hz), having a spectral composition similar to long-period events. Swarms of overlapping and very similar log-period events preceded the magmatic phase of Guagua Pichincha volcano in September 1999 (Villagomez et al., 2003). A similar tremor type, spasmodic tremor, is formed by sequences of merging

volcano-tectonic events such as occurred before Kelut eruption in 1990 (Lesage and Surono, 1995). Time lags between pulses are fairly constant in each episode with some spacing increase usually at the end of the episode. The tremor episode of May 6, 2002 shows an increase of the spacing from 13 s along most of the episode to 36 s at the end of the episode.

Different rapid-fire tremors show a large range of separation between pulses, taking into account only the more constant part. Larger spacing was observed on June 4, 2003 with 330 s between pulses. The shortest spacing was observed during the episode of July 2, 2003 with 0.7 s at the beginning of the episode to 1.4 s at the end.

The very repetitive and periodic character of these events suggests that they are related to a repeating non-destructive process. Duration of these sequences are variable. The tremor episode of June 7, 2003 has the shortest duration (160 s). No infrasonic signal accompanies or follows tremor episodes in areas with rapid-fire. This characteristic suggests a tremor episode not linked to explosions in the crater interior.

Some comments on the more interesting rapid-fire episodes are :

## May 06, 2002 15:12 Episode

Observed at the tremor episode of 2002 05 06 from 15:12 to 15:22 after two pulses of tremor with larger amplitudes and two gliding spectral lines. Repetitive pulses have the same spectral lines with peaks at 1.5 and 3.0 Hz.

January 18, 2003 11:06 Episode

An harmonic tremor episode with chaotic spectral pattern was followed by a sequence of 6 pulses of tremor. These pulses are spaced about 90 s apart. Duration of each pulse is around 60 s. Frequency content of these pulses is similar to the tremor suggesting that these events are long-period events originated in the same source that precedes a tremor episode. No acoustic signal was observed with this event.

February 01, 2003 Episode

An episode of rapid-fire tremor composed of 15 pulses was recorded at 11:28 following a tremor with a wide spectral content. Pulses occur at intervals of 30 s and show similar amplitudes and waveforms (Fig. 4.11). Spectral content seems to be similar to the tremor. No acoustic signal was observed with this event.



Fig. 4.11 Rapid-fire tremor recorded on 1 Feb. 2003 on the vertical component of E1S and MAC. Upper plots contain the velocity signals and lower ones show the spectrograms. Large spectral peaks are concentrated is the 2-4 Hz band.

June 07, 2003 02:43 Episode

A rapid-fire tremor episode occurred from 02:43 to 03:03 with 20 shocks during this period (1 pulse/min). Amplitudes show a slow increase up to the middle of the period and then a slow decreased. A large separation between events also occurs when amplitudes are small. Most of the energy is concentrated in the band between 0.9 to 1.3 Hz.

This rapid-fire tremor follows a low-frequency and small-duration tremor. It is composed by two parts with different amplitudes. This first one lasts 15 min and has 47 pulses (around 1 pulse / 20 s). All pulses are equally spaced and has the same order of amplitude. The second part with a duration of 18 min, has smaller amplitudes but the spacing remains very similar (1 pulse / 19 s). Both parts have the same spectral pattern with the main peak at 1.3 Hz and two very small overtones at 9.0 and 11.0 Hz (Figs. 4.12 and 4.13).



Fig. 4.12 Seismic signals recorded on MAC (2.1 km from crater) and BOM (6.95 km from crater) showing a rapid-fire tremor with 47 pulses distributed in two parts, the first one with higher amplitudes and the second part with smaller amplitudes. At time 515 and 1800 s there are two impulsive and short duration seismic signal, likely related to icequakes.



Fig. 4.13 Close-up of seismic signals of rapid-fire tremor recorded on June 19 2003 on BOM and MAC (Upper panel). Amplitudes are corrected for instrument magnification. A band pass filter was applied in order to remove aliasing effects (low-pass: 15 Hz) and microseismic noise (high-pass: 0.8 Hz). Power spectral density of both signals was computed using Thomson multitaper method.

## July 02, 2003 16:02 Episode

This is the longest rapid-fire tremor recorded on Erebus with a total duration of 210 min. (Fig. 4.14). Pulses have similar waveforms, again suggesting a very repetitive mechanism. Spectrograms show all overtones equally spaced, and looking like harmonic tremor rather than rapid-fire tremor (Fig. 4.14). Very slight gliding is also observed. Detailed spectral analysis shows up to 40 overtones in some portions of the episode (Fig.

4.15), with an apparent fundamental frequency of 0.25 Hz, although along most of the signal, a more consistent fundamental frequency around 0.5-0.6 Hz is observed. Despite their different distances to crater, the same spectral peaks are observed both at ABB (9.6 km to crater) and SBA (40 km to crater), with only changes in the amplitudes due to attenuation of high frequency overtones. During this episode, the number of shocks per time changes from 43 pulses per minute to 84 pulses per minute. Sometimes these pulses merge in a chaotic tremor type and also there are subtle changes in amplitudes along the episode.



Fig. 4.14 One-minute window time of rapid-fire tremor recorded on July 2, 2003 by vertical components of ABB short-period station and SBA broad-band station. Upper panels show the velocity time series and lower panels show the corresponding spectrograms.



Fig. 4.15 Multitaper pmtm power spectra of the rapid\_fire tremor of July 2, 2003 since 16:37 to 16:38 at ABB short-period station. Forty one equally-spaced spectral peaks are recognized.

#### 4.5 Correlation with explosive activity inside the crater

Commonly, it is accepted that there is a direct relationship between eruptive activity and tremor amplitude or duration. Some volcanoes, such as Etna (Alparone et al, 2003), show a drastic increase of tremor activity at the same time as there is an increase of eruptive activity. However, other volcanoes may have different behavior. At least at this level of activity, Erebus volcano shows a month-scale inverse relation between tremor occurrence and number of explosion-like events (Fig. 4.1). Tremor episodes are

more likely to occur when the volcanic conduits and vents are sealed or partially sealed. Meanwhile Erebus, an open-vent system, has a almost continuous degassing with sequestration, ascent and decompression of gas slugs with radii up to 5 m and the subsequent generation of strombolian explosions mainly through the lava-lake crater (Aster et al, 2003a). Williams-Jones et al. (2001) point out that Arenal volcano, another open-vent system, also exhibits an inverse correlation between frequency and magnitude of the explosive eruptions on the one hand, and occurrence of tremor on the other.

In order to confirm this relationship between tremor and crater activity, we examine video-records obtained by an infra-red camera located on the northern rim of Erebus from two time periods: January 25 to February 25, 2001, and January 11 to 27, 2002 (Fig. 4.16). During the first period, there was a burst in tremor activity with 16 events from February 2 to February 11. A low-level of tremor activity was observed during the second period with 4 episodes. Video observations allow us to discriminate the source vent of explosions as well as qualitatively assess of explosion size, based upon an estimation of the radii of swollen bubbles associated with explosions. Three vents were active during both periods, namely: Inner Crater, Ash-vent and Werner's craters. New vents became active during the second period: D-vent associated with ash-type explosions and B-vent with steam columns. Fig. 4.16 shows the largest size of volcanic explosions for each vent as well as the daily number of tremor episodes and the maximum velocity recorded on the vertical component of the nearest station to the crater (E1S). The upper-left panel shows a slight decrease in the size of lava-lake explosions which occurred since day 33 (Feb. 2, 2001) and an increase of the number of bubble bursts from Werner's crater and sporadic explosions from Ash-vent. At the same time, in the lower-left panel, there is a sharp increase in number and amplitude of tremor episodes that begins on day 33 (Feb. 2, 2001). On the other hand, during the second period, there is a steady decrease in the size of explosions (upper-right panel) with a small increase of tremor occurrence at the end of this period (lower-right panel).

From these observations, we should note that tremor activity at Erebus is not directly related to shallow processes, such as strombolian explosions or degassing. Tremor does not follow explosions on a time scale of minutes as was observed at Arenal (Williams-Jones, 2001). Post-eruptive tremor at Arenal was noted by Benoit and McNutt (1997), Garces et al. (1998) and also at Karymsky (Johnson et al. 1998). In those volcanoes emissions are followed by harmonic tremor and a sequence of repetitive acoustic pulses called chugs.



Fig. 4.16 Upper panels show video observations of crater activity using an infrared camera and the number of tremor episodes recorded by MEVO network with the largest amplitudes recorded on the vertical component of broadband station E1S, the station closest to the crater (lower panels). Data corresponds to two time periods: January 25 to February 25, 2001 (left panels) and January 11 to 27, 2002 (right panels). During the first period, there was a burst in tremor activity with 16 events from February 2 to February 11, 2001.

# 5. LOCATION OF TREMOR SOURCES

#### 5.1 Importance of source location

Location of tremor source is very important in volcano seismology. Epicentral solutions help us to identify active areas or active vents. Source depth might allow us to discriminate the processes occurring inside a volcano. Shallow source close or just on the vent are associated with magma degassing (Benoit and McNutt, 1997, Jonhson and Lees, 2000, Ripepe et al., 2001) or lava fountaining (Swanson et al., 1979, Dvorak and Okamura, 1985, Alparone et al., 2003). However, deep source tremors are likely related to magma/fluid transport processes without clear or direct manifestation on the surface. In all these mechanisms, seismic vibrations are radiated as elastic seismic waves. In this sense, tremor offers important information about the volcano's structure and dynamics. Tremor source location could be useful for mapping the extension and geometry of the underlying magma, conduits, or reservoirs, and also for quantifying pressure transients caused by resonance or movement of fluids along those conduits.

Tremor location faces problems from unclear onset times due to emergent arrivals and quasi-stationary character, making the use of classical seismic methods based on inversion of sets of arrival times inadequate (Hofstetter and Malone, 1986). Furthermore, high heterogeneity of volcanoes, and strong local effects (site and topography) may add significant non-source features to the seismogram. Here, several non-traditional seismic methods have been carried out. Many previous attempts have been made using amplitude and phase characteristics of tremor signals. Battaglia el al. (2001) located tremor events under Piton de la Fournaise using the coherency of the spatial amplitude distributions. Jolly et al. (2001) used *rms* amplitude distribution for locating tremor episodes on Monserrate volcano. Other methods are related to small time shifts of tremor waveforms using semblance or cross-correlation. Kawakatsu et al. (2000), Yamamoto et al. (2002), and Almendros et al. (2002), among others, used the semblance technique to locate tremor and LP events by measuring the coherency among seismograms. Cross-spectral methods may alternatively be used to find a relative location of multiplets (Poupinet et al., 1985, Fremont and Malone, 1987, and Lesage and Surono, 1995). Legrand et al. (2000) located long-period signals at Aso volcano computing waveform linear inversions of seismograms with 10 broadband stations. Most of these methods require extensive seismic arrays with high dynamic broadband instruments, and only few attempts have been made for locating volcanic tremors using permanent monitoring-based seismic networks (Wassermann and Ohrnberger, 2001).

In this study non-traditional techniques such as semblance, envelope-based and spectral cross-correlation, and iso-seismal distribution have been applied in order to constrain the source location of tremor episodes recorded at Erebus volcano using the MEVO seismic network. 5.2 Description of methods for locating tremor sources at Erebus

Four methods were applied for locating tremor sources at Erebus volcano: Analysis of iso-seismal surfaces, semblance, cross-correlation of signal envelopes, and cross-correlation of signal spectrograms.

5.2.1 General assumptions for locating tremor episodes at Mt. Erebus

Several assumptions were applied for locating tremor episodes at Mt. Erebus:

- 1) Tremor wavefield is composed of p-waves with a velocity of (3.80-4.07) km/s propagating through a homogeneous medium.
- 2) Waves are radiated from the source in the same way in all directions (isotropic radiation).
- 3) Attenuation is controlled by geometric spreading.
- 4) Site and topographic effects are neglected.
- 5.2.2 Iso-seismals distribution method

Seismic signals lose energy along their travel path due to geometric spreading and intrinsic attenuation. It is thus expected that signal amplitude decays with greater distance from the source. High amplitude signals indicate that the source is nearby while lower amplitude signals indicate that the source is more distant. The far-field P-wave attenuates according to the inverse of the distance r (Aki and Richards, 1980). Nearfield oscillations have stronger attenuation coefficients.

Amplitude distribution has been used in a trial location, where  $A_o$  is calculated for each grid-node and for each station. The minimum residual of *rms* corresponds to the best agreement between the amplitude data from all stations (Jolly et al., 2001). Gottschammer and Surono (2000) applied a grid based method in order to locate the tremor source at Bromo volcano using as the distance-dependent parameter the power of the velocity signal. Kanamori (1993) postulated a method using known accelerationdistance relations.

In this study we plot the rms amplitude values of velocity recorded in each station for selected portions of tremor time series, and we contour the amplitude distributions using Surfer 7.0 software.

#### 5.2.3 Semblance method

The semblance technique (Neidel and Taner, 1971) is a coherence measurement between different pairs of seismic signals. Semblance denotes the ratio of the total energy of the stack within a gate of length (1+L $\Delta$ ) to the sum of the energy of the component traces within the same time gate (Sheriff and Geldart, 1995).

$$S_{k} = \sum_{j=1}^{L} \left[ \sum_{i=1}^{N} (v_{i,ji}) \right]^{2} / \left\{ N \sum_{j=1}^{L} \left[ \sum_{i=1}^{N} (v_{i,ji}^{2}) \right] \right\}$$
(5.1)

where *N* is the number of stations,  $v_{i,j(i)}$  is a seismogram recorded at the *i*th station in the *j*th time sample and *L* is the number of samples that defines a sliding time window. This method considers that the largest coherence corresponds to the arrival of common phases at different stations with different time delays. These time delays can be found by changing the source location in a 3-dimensional grid of nodes. Larger semblance values are found where the time shifts produce the best coherence between seismic signals.

A Matlab code semblance.m was written by myself and D. Wilson in order to find the largest semblance values in a 50x50x90 node grid around the volcano, bounded by the coordinates -77.7° and -77.3° South, and 166.6° and 167.6° East, with depth steps of 200 m. Shift times are calculated according to each trial position of the source in the grid-search, assuming direct rays. The total signal is spliced in *m* windows. The semblance value is then calculated for each set of the  $k_{th}$  window corrected by the corresponding time shifts. The grid location with the highest semblance  $S_k$  will give the best estimate of the coordinates (latitude, longitude and depth) of the tremor event. A weighted median value of these partial coordinates is computed using the corresponding  $S_k$ . Error bars were calculated at 95% of confidence using a bootstrap algorithm that randomly generates a series of latitude, longitude and depth values weighted by  $S_k$ .

The semblance method has been used for estimating the tremor source at Izu-Oshima volcano (Furamoto et al., 1990, 1992) taking advantage of a multichannel array deployed near the crater (small arrays are adventageous in this technique because they produce highly coherent seismograms). An expanded version of the semblance technique that considers the strong rectilinearly exhibited by long-period signals, has been adapted for locating long-period volcanic tremor at Usu (Yamamoto et al., 2002), at Aso (Kawakatsu et al., 2000), at Arenal (Hagerty et al., 2000) and at Kilauea (Almendros et al., 2002).

5.2.4 Cross correlation of signal envelopes

Some harmonic tremors present amplitude modulated envelopes (beating effects) in all stations around Erebus, suggesting that this effect is a source-process. Envelopes of signals showing beating effect will offer a smooth representation of these episodes. These envelopes are calculated using the absolute value of the Hilbert transform of the corresponding time-series. A smoothing function was applied to the envelope curve in order to reduce the effect of spikes. The complete time window was divided in 20 windows with 80% overlap and each of these windows were cross-correlated with corresponding windows of other stations.

Since the cross-correlation function can be used as a measure of the coherence between different seismic signals, we compute an average of cross-correlation of all subwindows for each pair of stations in order to find the delay time matrix for the arrivals delays.

Predicted time delays were calculated using straight rays in an isotropic media from each point of a dense grid to the seismic stations. Tremor source location was determined minimizing the residual between the delay times found with cross-correlation and the calculated delays using the grid search (difference between observed and predicted travel times).

Each grid point is assigned a value corresponding to the reciprocal of the residual of the observed minus the predicted travel time for that grid point, so that the maximum value is the grid location with the smallest residual. This approach works well in signals with variations in amplitude.

A high pass (0.5 Hz) filter was applied in order to remove the effect of microseismic noise from the signal. A low pass filter was used above the fundamental frequency. In case of chaotic signals (without a spectral peak), a 10 Hz low pass filter was applied in order to prevent aliasing effect. Stronger filters around the fundamental frequency were occasionally applied.

A grid search was performed in order to find the location that best fits the observed time lags. A matlab code xcorr\_search.m written by myself and D. Wilson computes time lags for each pair of stations, then performs the grid search. Travel times from each grid node to each station are computed using a uniform velocity of 3.8 km/s. In the following grid searches, we have used a 50x50 node grid bounded by the coordinates  $-77.7^{\circ}$  and  $-77.3^{\circ}$  S, and  $166.6^{\circ}$  and  $167.6^{\circ}$  E, with depth steps of 100 m.

5.2.5 Spectral Cross-correlation

Spectrograms are a 3-D visualization of tremor episodes. Time is plotted in the abscissa, frequency in the ordinate, while amplitude is plotted with a color scale.

Spectrograms are calculated for moving windows of 256 points of each seismic signal with an overlap of 255 data points. For each point of the time series, a matrix containing the spectrogram of each moving window is computed. Each *jth* column of signal spectrogram is composed of *i* frequency values. A cross correlation between the correspondent frequency values of each pair of spectrograms is computed. The time lags between different stations are considered the observed delay times. We will also apply a grid search to find the location of the source of selected tremor episodes.

#### 5.3 Validation of tremor location methods

Tremor location methods were validated using a synthetic signal of 100 s (Fig. 5.1), that contains a scaled and time-shifted real tremor signal recorded by the vertical component of broad-band CON station. This tremor signal has a clear onset and a gliding fundamental frequency. CON.BHZ signal was copied on the rest of the seismic signals belonging to Erebus network using appropriate arrival times for direct rays from the real hypocenter (77.5° S - 167.2° E) to each of the stations and a constant velocity of 3.80 km/s. Table 5.1 shows the calculated delay times for the theoretical tremor source.

Tremor amplitudes were also modified in order to match the attenuation pattern of body waves. The master signal (CON.BHZ) was normalized and a correction factor of the inverse of the source-station distance (1/r) was introduced for all stations, so the final signal contains a hypothetical time lag and amplitude (Fig. 5.1).

STATION	DELAY(s)	STATION	DELAY (s)
ABB	2.28	НОО	2.01
BOM	1.63	LEH	0.99
CON	1.54	MAC	1.33
E1S	1.38	NKB	1.17
HEL	0.91	SBA	10.59

Table 5.1 Delay time at each seismic station for a synthetic tremor signal. Signal source was located at the sea level with epicentral coordinates:  $77.5^{\circ}$  S -  $167.2^{\circ}$  E. A isotropic source that generates p-waves and a homogeneous half-space with a velocity of 3.8 km/s, were considered for this analysis.



Fig. 5.1 Synthetic tremor generated using a master signal with amplitude and time lag corrections according to a source located at  $77.5^{\circ}$  S,  $167.2^{\circ}$  E and 3.7 km depth. Time lags are shown in table 5.1. Amplitude corrections follows a 1/r attenuation factor.

#### 5.3.1 Semblance method

The semblance method was applied over a 100-s window of the synthetic signal. Seismic signals were filtered with a butterworth band-pass filter of 1.0 to 5.0 Hz which keeps the energy of this type of events. The largest coherence point was located at the sea level (0 m), at the coordinates 77.50° S and 167.21° E (Fig. 5.2). This point has an error of 156 m in latitude and 146 m in longitude with respect to the real location of the synthetic signal. These errors are smaller than half of the grid spacing (519 m in latitude and 432 m longitude). No errors were found in depth determination.



Fig. 5.2 Semblance analysis of a 100-s window of a synthetic tremor signal. Upper left panel shows the entire signal and the 100-s. window used for this analysis. A butterworth 1.0-5.0 Hz band-pass filter was applied. Right-upper panel shows a cross-section at the highest semblance level. Lower panels show the E-W and N-S cross sections containing the maximum semblance point. Color bar at lower panels shows the semblance scale with high coherence values.

#### 5.3.2 Method of cross-correlation of envelopes

The cross-correlation of the envelopes was applied to a 100-s window around the first pulse. Signals were filtered with a butterworth band-pass filter of 1.0 to 5.0 Hz. SBA signal was used because it caused large errors. Maximum correlation was found beneath the northern part of the summit plateau, at 77.50° S and 167.17° E (Fig. 5.3) and
4,200 m below sea level. This point is inside a narrow high correlation area that extends from 3 to 6 km below sea level. Small relative arrival times (<0.15 s) explain the deep location of tremor source. The maximum correlation point has an error of 201 m in latitude and 686 m in longitude with respect to the real location of the synthetic signal. The latitude error is smaller than the latitude grid spacing (519 m) but the longitude error is larger than longitude grid spacing (432 m). Depth error (> 100%) is quite significant in this method.



Fig. 5.3 Cross-correlation of signal envelopes method applied to a synthetic signal with origin at 77.5° S and 167.2° E and 3.7 km below crater floor (at sea level). Upper left panel shows envelope signals calculated using the Hilbert transform. Upper right panel shows in color the topographic distribution of Erebus. Diamonds denote the seismic stations and the star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section. Color scale in lower section is gives the reciprocal of the residual of the predicted vs. the observed delay times.

5.3.3 Method of cross-correlation of spectrograms

Cross-correlation of spectrograms was performed over the synthetic signals with a window time of 100 s and the same butterworth bandpass filter 0.5-5 Hz. All these signals contain a clear gliding effect with the fundamental frequency changing from 3 to 5 Hz. A stable solution was located beneath the crater area at the sea level (3,700 m below the crater floor, Fig. 5.4). Comparing with the coordinates of the hypothetical signal, errors of around 200 m were found in latitude and longitude. These values are smaller than the grid resolution (half of the grid spacing) in both cases. No errors were found in depth. Using synthetic signals without gliding effect, errors larger than grid spacing were found.



Fig. 5.4 Cross-correlation of signal spectrograms of the synthetic tremor. Upper left panel shows the complete raw signal and the 100 s data window analyzed. Upper right panel shows in color the topographic distribution of Erebus, the seismic station (diamonds), and the epicentral location of the highest correlation value (star). Lower panels show the N-S and E-W cross section. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

# 5.3.4 Summary

A synthetic signal facilitated a validation of three methods for locating tremor episodes using the seismic network installed at Erebus volcano. These signals contain a gliding fundamental frequency, scaled amplitudes and onset times according to the hypocentral distance. This is a summary of the results:

- Solution obtained with the semblance method was very close to the source point.
  Errors were smaller than the grid resolution (half of node separation) and no error was found in the depth determination.
- Using the cross-correlation of signal envelopes with nine seismic stations, except SBA, we found an error smaller than the node spacing in latitude and a larger error in longitude. A large error was also found in depth determination. Despite these errors, the hypocentral solution obtained with this method is stable and roughly point the correct epicentral area.
- Cross-correlation of spectrograms offers a good and stable solution with small errors in latitude and longitude and no errors in depth determination. This method is adequate for signals with frequency variations (gliding). Applying this method on signals with constant frequency may become highly unstable.
  - 5.4 Location of tremor episodes

Four tremor episodes from January 1st to April 12th, 2003 were selected for a location analysis based upon the following characteristics:

a) Tremor episodes should be recorded by all seismic stations of Erebus network, including broad-band stations installed on the 2002-2003 field season (NKB, LEH, CON, and HOO). This consideration bounds the analysis only to tremor episodes occurred

during the period between January and April 2003. After April 2003, some seismic stations faced power supply problems.

b) Signals should have enough energy in order to have high signal-to-noise ratio in all stations of Erebus volcano, even at SBA station located at 38 km from the crater.

c) No clipping amplitudes in short period stations of Erebus network, which distorts the waveform and spectrum of the event. Combining the characteristics (b) and (c), the tremor episode should be large enough in order to be recorded in SBA and small enough for avoiding the amplitude saturation effect at the short-period stations.

d) Different tremor types (harmonic, chaotic and rapid fire) will be located.

We will define tremor sources locations when there is agreement between different locating methods. Two harmonic events (02/02/03 and 04/12/03), and two rapid-fire tremors (01/18/03 and 02/01/03) will be located using the described methods.

5.4.1 Location of 02/02/03 Harmonic Tremor Episode

This episode started at 15:10 UT and has a duration of 2,550 s (Fig. 5.5). It shows a transition between a first part with very constant fundamental frequency of 1.3 Hz, five equally-spaced overtones and beating effect and a second part with a diffuse spectra where the overtones are difficult to identify. The first part lasts about 1,500 s.



Fig. 5.5 Harmonic tremor episode recorded on Feb. 2, 2003 by 10 seismic stations of Erebus network. Only vertical components are plotted. Amplitude are given in  $\mu$ m/s. Signals are band-pass filtered in the range 1.0 - 2.0 Hz.

# 5.4.1.1 Iso-seismal distribution

Signal amplitudes in Fig. 5.5 show larger values for stations HEL, NKB, and MAC located around the crater. The farther from the crater the stations are located, amplitudes tend to decrease. An iso-seismal plot using the *rms* values of signal amplitude calculated for a 40-s window show also large amplitudes in stations located on the northern flank (HEL, NKB and MAC) as well as around the crater.

A plot of rms amplitudes of the entire signal filtered around the fundamental

frequency 1 Hz  $< f_0 < 2$  Hz shows that the tremor source is likely located beneath the upper southern flank (Fig. 5.6). Amplitude distributions over time windows of 100 s also have a consistent a peak of high amplitudes beneath the upper part of the southern flank.



Fig. 5.6 Distribution of *rms* amplitudes calculated for the complete signals of harmonic tremor recorded on Feb. 02, 2003. Contouring was performed with radial-based functions of Surfer software. Location of seismic stations is denoted by diamonds and normalized *rms* amplitude are located close to the stations with vertical numbers. Iso-seismic curves are drawn every 0.1. Despite some inconsistencies, i.e. HEL, station that has the largest *rms* value, the larger amplitude area is located on the upper southern flank of the volcano. Color bar shows the scale of normalized amplitudes.

The best fit between the theoretical and observed ratios of *rms* amplitudes of ABB, BOM and SBA relative to the vertical component of E1S, was found for a hypothetical hypocenter located at 77.56° S and 167.15° E and 8.6 km beneath the summit (Fig. 5.7). This point corresponds to a source at intermediate depth below the upper southern flank.



Fig. 5.7 Observed ratios between *rms* amplitudes of BOM, ABB and SBA with respect to E1S for the tremor episode of 02 Feb. 2003 and theoretical curves showing the amplitude ratios for different depths. At some depths (marked by arrows), these theoretical curves intercept the observed ratio, constraining the point where the tremor source is likely located.

#### 5.4.1.2 Semblance method

A grid search was performed based on the semblance method over a 100-s

window after the onset with a butterworth band pass filter of 1.0 to 2.0 Hz which keeps the energy of the fundamental frequency. The largest coherence point was located at 1.8 km below sea level, at the coordinates 77.503° S and 167.206° E, at the northeaster rim, inside a zone of high coherence that extends from 0.5 km to 2 km beneath the sea level (Fig. 5.8). This area corresponds to a source located at intermediate depth beneath the caldera area. With a very large window (1400 s), the best coherence solution is located close to the crater at  $3.4 \pm 0.2$  km beneath summit.



Fig. 5.8 Distribution of semblance values for a 100-s window of tremor episode of 02 February 2003. Semblance scale is shown in color-bars with higher semblance values in red color. Upper left panel shows the entire tremor episode and the tremor window analyzed with this method. Upper right panel shows the semblance distribution at 1.2 km beneath sea level. Lower panels show the semblance N-S and E-W cross-sections.

The cross-correlation of the signal envelope computed for a 100-s window beginning at the tremor onset gives a maximum value beneath the north rim of the summit plateau, inside a narrow zone deeper than 8 km beneath the summit (Fig. 5.9). Epicentral coordinates of the tremor source are 77.51° S and 167.15 E°. Small relative arrival times (<0.02 s) explain the deep location of tremor source.



Fig. 5.9 Cross-correlation of signal envelopes method applied to Feb. 02, 2003 tremor episode. Upper left panel shows envelope signals calculated using the Hilbert transform. Upper right panel shows in color the topographic distribution of Erebus. Diamonds denote the seismic stations and the star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section. Color scale in lower section is gives the reciprocal of the

# residual of the predicted vs. the observed delay times. 5.4.1.4 Spectral cross-correlation

Using a window time of 140 s beginning at the onset of the episode and a butterworth bandpass filter 1-9 Hz, a stable solution was located at 11 km beneath the upper north flank (Fig. 5.10). Results are unstable if larger time windows are analyzed. Very high time residuals are found between station with the earliest arrival and the other ones, meanwhile arrivals between them are almost identical arrivals. The solution became more stable after excluding the station Bom because its anomalous arrival times.



Fig. 5.10 Cross-correlation of signal spectrograms applied to Feb. 02, 2003 tremor episode. Upper left panel shows the complete raw signal and the 140 s window analyzed. Upper right panel shows in color the topographic distribution of Erebus. Diamonds denote the seismic stations and the star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

Amplitude based methods, such as distribution of iso-seismals and attenuation fitting give a source located around the crater area or upper southern flank at 8 km below the summit. Semblance and cross correlation methods locate the source beneath the crater or the upper part of the northern flank, with a 3-4 km depth according to semblance searches and a deeper (>10 km) source with cross-correlation methods.

## 5.4.2 Location of 04/12/03 Harmonic Tremor Episode

The tremor episode occurred on April 12, 2003 has basically two parts, the first one lasts 35 min, and has a fundamental frequency at 0.7 Hz and 5 overtones clearly seen. The second part has a more chaotic behavior and no overtones are recognized. Location methods will be applied over the first part which contains the harmonic part the follows the tremor onset (Fig. 5.11).



Fig. 5.11 Harmonic part of the tremor episode recorded on Apr. 12, 2003 with 35 min duration (2100 s). This part is followed by a non-harmonic small-amplitude part (not shown in this figure). Location techniques are applied over a 100-s. window bounded by two vertical bars at the beginning of the episode. For semblance method, a data window of 200 s was used. Amplitudes are true velocity ground motions in  $\mu$ m/s.

## 5.4.2.1 Iso-seismal distribution

*Rms* values of amplitudes were computed on a 100-s window shown in Fig. 5.11. These values were normalize and plotted for all stations. Iso-seismal curves drawn using radial-based functions of Surfer software show a zone with high amplitudes located around the station HEL located on the upper part of the northern flank of Erebus edifice (Fig. 5.12).

#### RMS AMPLITUDE DISTRIBUTION TREMOR EPISODE 04/12/03 06:48



Fig. 5.12 Distribution of *rms* amplitudes calculated for a 100-s window of harmonic tremor recorded on Apr. 12, 2003. Contouring was performed with radial-based functions of Surfer software. Location of seismic stations is denoted by diamonds and normalized *rms*. amplitude are located close to the stations with vertical numbers. Iso-seismic curves are drawn every 0.1. Larger amplitude area is located on the upper northern flank of the volcano.

The best fitting between the theoretical and observed ratios of *rms* amplitudes ABB, BOM and SBA relative to the vertical component of E1S, was found for a hypothetical hypocenter located at  $77.503^{\circ}$  S and  $167.206^{\circ}$  E and 4.2 km beneath the summit (Fig. 5.13). This point is 0.5 km below sea level. Its epicenter corresponds to the



Fig. 5.13 Ratios between *rms* of amplitudes of BOM, ABB and SBA with respect to E1S for the harmonic tremor episode at 12 Apr. 2003 and theoretical curves showing the amplitude ratios for different depths at a selected point, called epicenter: 77.503° S and 167.206° W. At 4.18 km (average of marked points), these curves intercept, defining the depth point where observed amplitudes agree with theoretical attenuation ratios.

#### 5.4.2.2 Semblance method

The semblance method was applied over a 200-s window which starts at the beginning of this episode. Seismic signals were filtered with a butterworth band pass filter of 0.8 to 3.0 Hz which keeps most of the energy of this event. The largest coherence point was located at 3.0 km below sea level, at the coordinates 77.527° S and

167.078° E (Fig. 5.14). This area corresponds to a deep source with epicenter close to CON station, in the SW rim of the sommital caldera. Choosing a window length of 2800 s spliced in 280 windows, the highest coherence is reached at 3200 m deep, below the northern caldera rim.



Fig. 5.14 Semblance analysis of a 200-s window of the harmonic tremor of Apr. 12, 2003. Upper left panel shows the entire raw signal and the data window used for this analysis. Signal was filtered with a butterworth 0.8-3.0 Hz band-pass filter. Right-upper panel shows a cross-section at 3,000 mbsl., at the level where the highest semblance was found (at coordinates 77.527° S and 167.078° E). Lower panels show the East-West and North-South cross sections containing the maximum semblance point. Color bar shows the semblance scale.

#### 5.4.2.3 Envelope cross-correlation

The cross-correlation of the signal envelope was computed for a 100-s window

that contains the beginning of the harmonic tremor. The maximum cross-correlation point is located on the coordinates  $77.528^{\circ}$  S and  $167.238^{\circ}$  E at a depth larger than 10 km (Fig. 5.15). This point is located inside a narrow zone of high coherence bounded by coordinates  $77.50^{\circ}$  to  $77.55^{\circ}$  S and  $167.2^{\circ}$  to  $167.3^{\circ}$  E, which is dipping to the East.



Fig. 5.15 Cross-correlation of signal envelopes method applied to Apr. 12, 2003 harmonic tremor episode. Upper left panel shows envelope signals calculated over a 100-s window using the Hilbert transform. Upper right panel shows in color the topographic distribution of Erebus. Diamonds denote the seismic stations and star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section with a vertical exaggeration of 2. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

#### 5.4.2.4 Spectral cross-correlation

Cross-correlation of spectrograms was performed over seismic signals with a window time of 100 s beginning at the onset of the episode and a butterworth bandpass filter 0.5-4 Hz. All these signals contain at least 4 clearly spaced harmonics. A stable solution was located beneath the crater area at shallow depth (3,000 m above sea level, Fig. 5.16). Results are unstable if different time windows are analyzed. Very large time residuals are found between station with the earliest arrival (BOM) and the other ones, meanwhile arrivals between them are almost identical arrivals. We relocated the event excluding the station with an anomalous arrival (BOM) and finally the solution became more stable but with a smaller number of stations.



Fig. 5.16 Cross-correlation of signal spectrograms applied to Apr. 12, 2003 harmonic tremor episode. Upper left panel shows the complete raw signal and the 100-s window analyzed. Upper right panel shows in color the topographic distribution of Erebus. Diamond symbols denote the seismic stations and star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

#### 5.4.2.5 Summary

The cross-correlation of spectrograms locates the Apr. 12, 2003 tremor close to the crater. Semblance methods applied over the complete signal gives the highest coherence at 3.2 km below the LEH station (northern caldera rim). Epicenter obtained by cross-correlation of envelopes is located also in the same area, however solutions have different depths. Cross-correlation of envelopes gives a deep solution (>14 km beneath

summit), cross-correlation of spectrograms, a shallow solution (< 2 km), and semblance an intermediate one (~3 km). This discrepancy in the depth of the source could be solved looking at an independent method based on a comparison of attenuation ratios between amplitude *rms* of independent station (ABB, BOM. SBA), and a reference station (E1S), which gives the best fitting solution for a point located at 3.8 km below the summit. This solution will be also in agreement with the distribution of iso-seismals around a point close to the NE edge of the summit plateau.

#### 5.4.3 Location of 01/18/03 Rapid-Fire Tremor Episode

Four methods were applied in order to locate the source of 01/18/03 Rapid-Fire Tremor. As it was mentioned in section 4.4.3, this episode is composed of seismic pulses with a 90-s separation. Most of the energy is concentrated on a 1 to 2.0 Hz band. Fig. 5.17 shows the seismic signals on vertical components of Erebus network with the rapidfire part starting at time 720 s.

#### 5.4.3.1 Iso-seismal distribution

*Rms* amplitudes were computed for the entire rapid-fire tremor signal in a 1-2 Hz band and normalized to 1. Largest amplitudes are located at HEL, MAC, NKB and BOM, and lower amplitudes at ABB, HOO and finally SBA. Contouring these amplitudes with radial-based functions of Surfer software, gives a bull-eye shape distribution with a maximum located at the NE part of the summit plateau, close to Fang Ridge (Fig. 5.18).



Fig. 5.17 Rapid-fire tremor of Jan. 18, 2003 following a chaotic tremor episodes. Six pulses are clearly seen in all stations with a 90-s separation between them. Amplitudes are true velocity ground motions in  $\mu$ m/s.

Isoseismal solution shows an elongation in NNE-SSW direction and it is very well constrained in the EW plane. Maximum *rms* area for a 100-s window remains in the same area at the NE flank.

The best fitting between the theoretical and observed ratios of rms amplitudes ABB, BOM and SBA relative to the vertical component of E1S, was found for a hypothetical hypocenter located at 77.485° S and 167.32° E and 5.2 km beneath the summit (Fig. 5.19). This point is 0.5 km below sea level. Its epicenter corresponds to the NE flank.



Fig. 5.18 Distribution of *rms* amplitudes calculated for the complete signals of rapid-fire tremor recorded on Jan. 18, 2003. Contouring was performed with radial-based functions of Surfer software. Location of seismic stations are denoted by diamonds and normalized *rms* amplitude are located close to the stations with vertical numbers. Iso-seismic curves are drawn every 0.1. Largest amplitude area

is located on the upper part of NE flank.



Fig. 5.19 Observed ratios between *rms* amplitudes of BOM, ABB and SBA with respect to E1S for the rapid-fire tremor 18 Jan. 2003 and theoretical curves showing the amplitude ratios for different depths. At some depths (marked by arrows), these curves intercept, constraining the point where observed amplitudes agrees with theoretical attenuation ratios.

#### 5.4.3.2 Semblance method

A grid search was performed based over a 100-s window from time 820 to 920 s after the tremor onset. Seismic signal was previously filtered with a butterworth band pass filter of 1.0 to 2.0 Hz which keeps most of the energy of the event. The largest coherence point was located at 0.4 km above sea level (3.4 km beneath summit, Fig. 5.20), at the coordinates 77.550°S and 167.206°E, inside a zone of high coherence that extends from 0.5 km above sea level to 0.2 km below sea level. This area corresponds to a source at intermediate depth beneath the SW flank. Semblance method computed over 7 windows of 100 s, each containing a pulse of the rapid-fire tremor, gives the best coherence at 0.3 km above the sea level beneath the western rim of the caldera.



Fig. 5.20 Semblance analysis of a 100-s window of the rapid-fire tremor of Jan. 18, 2003. Upper left panel shows the entire raw signal and the 100-s. window used for this analysis. Signal was filtered using a butterworth 1-2 Hz band-pass filter. Right-upper panel shows a cross-section at 400 m above sea level, where the highest semblance was found (coordinates  $77.55^{\circ}$  S and  $167.06^{\circ}$  E). Lower panels show the E-W and N-S cross sections containing the maximum semblance point. Cross section at 400 m also shows a high semblance area on the northern flank. Color bar shows the semblance scale.

#### 5.4.3.3 Envelope cross-correlation

The cross-correlation of the signal envelope was computed for a 100 s window that contains a pulse of rapid-fire tremor (from 4050 to 4150 s). The maximum cross-

correlation point is located on the northeastern upper flank the coordinates 77.49° S and 162.27° E at a depth larger than 10 km (Fig.5.21). Considering the next 100-s. *w*indow, the epicenter is located in north flank at 2,000 m above sea level. Other time windows (time 4200 to 4400 s and 1-6 Hz filter) gave a solution very close to HEL station, also on the NE flank.



Fig. 5.21 Cross-correlation of signal envelopes method applied to Jan. 18, 2003 rapid-fire tremor episode. Upper left panel shows signal envelopes calculated using the Hilbert transform. Upper right panel shows in color the topographic distribution of Erebus. Diamonds denote the seismic stations and the star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section with a vertical exaggeration of 2. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

A rapid-fire tremor source was located using a cross-correlation of spectrograms over a window time of 50 s beginning at the onset of the episode. Data was filtered using a 1-3 Hz butterworth bandpass filter. A stable solution for this time window is located at 10 km below sea level at coordinates: 77.5106° S 167.151° E (Fig. 5.22). Using small windows over a 1-6 Hz tremor signal we also obtain solutions on the north flank.



Fig. 5.22 Hypocenter coordinates  $(77.51^{\circ} \text{ S} \text{ and } 167.15^{\circ} \text{ E})$  were found using a 50s signal window and applying the cross correlation method of spectrograms. Upper-left panel shows the raw-data and the 50 s window after a 1-3 Hz butter band-pass filter. Right panel shows a color scaled topographic map with the location of seismic station (diamonds) and including the maximum correlation point with a star. High resolution areas are deeper than 6.3 km. Lower panels show the EW and NS cross-sections and adjacent color scale gives the reciprocal of the residual of the predicted vs. the observed delay times.

#### 5.4.3.5 Summary

The amplitudes distribution of the 01/18/03 rapid-fire tremor shows a source located below the NE flank, close to Fang Ridge. This epicenter is close to the points of maximum cross-correlation using the envelopes of the tremor signals. Source depth is likely 5 km beneath the summit according to the attenuation curves method. Semblance method locates this episode at 3.5 km beneath the southwestern rim, probably due to the difficulty of apply semblance in high-frequency seismic signals of Erebus. Epicentral location using cross-correlation of spectrograms gives a solution close to the crater at depth larger than 6.3 km.

## 5.4.4 Location of 02/01/03 Rapid-Fire Tremor Episode

This episode was briefly described on section 2.2.3. In this section, we apply the methods already described for locating the onset of the rapid-fire part of the 02/01/03 tremor. Signal spectrum of rapid-fire part shows that this event does not exhibited harmonics and most of the energy is concentrated on 1-6 Hz band (see Fig. 4.11).



Fig. 5.23 Rapid-fire tremor recorded on Feb. 01, 2003 on seismic stations of Erebus network. This episode has a total duration of 2,400 s. This plot contains only the last part of a chaotic tremor from time 0 to 420 s, and the rapid-fire tremor, composed by 16 shocks is recorded from time 420 to 900 s.

#### 5.4.4.1 Iso-seismal distribution

Amplitude values (*rms*) calculated for a 100 s window in the 1-6 Hz frequency band, show values larger than 4  $\mu$ m/s at stations located on the northern flank (HEL, NKB and E1S) and values smaller than 2  $\mu$ m/s for stations located on the south-western flank (CON, HOO) or very distant from the crater (SBA). This distribution suggests that the tremor source is located beneath the northern flank and close to the summit. A plot of *rms* amplitudes of the entire signal filtered around the fundamental frequency 1 Hz  $< f_0 < 2$  Hz shows that the origin is located beneath the upper southern flank (Fig. 5.24). Amplitude distributions over time windows of 100 s also have a consistent a peak of high amplitudes beneath the upper part of the northeastern flank.



#### RMS AMPLITUDE DISTRIBUTION RAPID-FIRE TREMOR EPISODE 02/01/03 11:00

Fig. 5.24 Distribution of rms amplitudes calculated for the complete signals of rapid-fire tremor recorded on Feb. 01, 2003. Contouring was performed with radial-based functions of Surfer software. Location of seismic stations is denoted by diamonds and normalized rms amplitude are located close to the stations with vertical numbers. Iso-seismic curves are drawn every 0.1. Largest amplitude area is located on the upper part of NE flank of the volcano, close to HEL station.

The best fit between the theoretical and observed ratios of rms amplitudes ABB, BOM and SBA relative to the vertical component of E1S, was found for a hypothetical hypocenter located at 77.51° S and 167.20° E and 4.2 km beneath the summit (Fig. 5.25). This point is 0.5 km below sea level. Its epicenter corresponds to the northern part of the



Fig. 5.25 Observed ratios between rms amplitudes of BOM, ABB and SBA with respect to E1S for the rapid-fire tremor episode at 01 Feb. 2003 and theoretical curves showing the amplitude ratios for different depths. At 4.18 km (marked by arrow), these curves intercept, defining the depth point where observed amplitudes agrees with theoretical attenuation ratios.

#### 5.4.4.2 Semblance method

Semblance method was applied over a 100 s window which starts at the beginning of the rapid-fire part. Seismic signals were filtered with a butterworth band-pass filter of 1.0 to 5.0 Hz which keeps the energy of this type of events. The largest coherence point was located at 0.6 km above sea level, at the coordinates 77.51° S and 167.19° E (Fig. 5.26). This area corresponds to a source located beneath the northern edge of the summit

plateau. However applying this technique over the whole rapid-fire part, the largest coherence was found at the upper NW flank at 0.3 km above sea level.



Fig. 5.26 Distribution of semblance values obtained for rapid-fire tremor episode of 01 Feb. 2003. Upper left panel shows the entire tremor episode and the filtered tremor window analyzed with this method. Upper right panel shows the semblance distribution at 0.6 km above sea level. Lower panels show the semblance N-S and E-W cross-sections. Semblance scale is shown in color-bars with blue colors denote low semblance values and high semblance with red-color.

## 5.4.4.3 Envelope cross-correlation

The cross-correlation of the signal envelope computed for a 100-s window around the second pulse of the rapid-fire tremor gives a maximum value beneath the NW flank of the summit plateau, between in a narrow zone deeper than 8 km beneath the summit. Epicentral coordinates of the tremor source are 77.49° S and 167.11° E (Fig. 5.27). The high correlation area dips to the East without variation on the N-S plane. Small relative arrival times (<0.02 s) explain the deep location of tremor source.



Fig. 5.27 Cross-correlation of signal envelopes method applied to Feb. 01, 2003 rapid-fire tremor episode. Upper left panel shows envelope signals calculated using the Hilbert transform. Upper right panel shows in color the topographic distribution of Erebus. Diamonds denote the seismic stations and the star is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

5.4.4.4 Spectral cross-correlation

Using a window time of 100 s beginning around the first pulse of the rapid fire tremor filtered with a butterworth bandpass filter 1-9 Hz, a stable solution was located at 10 km depth beneath the upper part of the north flank (Fang ridge). The area with high correlation is bounded by the coordinates 77.43° to 77.49° S and 167.1° to 167.3° E (Fig. 5.28). Cross sections show a small tilt to the East without variation on N-S plane. Results are unstable if different time windows are analyzed. Very high time residuals are found between station with the earliest arrival (BOM) and the other ones, meanwhile arrivals between them are almost identical arrivals. Excluding BOM the solution became more stable.

# 5.4.4.5 Summary

All methods - such as distribution of iso-seismals, semblance and crosscorrelation of envelopes, and cross-correlation of spectrograms - locate the episode on the northern part of the summit plateau or on the upper NW flank. Solution depth for the attenuation curve is 0.5 km beneath the sea level (4.2 km beneath the summit) and semblance gives a depth of 0.3 km above the sea level. Cross-correlation methods have a solution deeper than 10 km beneath sea level. Given the coincidence shown by attenuation curves and semblance, we consider that source depth is located around the base of the volcanic cone.



Fig. 5.28 Cross-correlation of signal spectrograms applied to Feb. 01, 2003 rapidfire tremor episode. Upper left panel shows the complete raw signal and the 60 s window analyzed (defined by a horizontal bar above the seismic trace). Upper right panel shows in color the topographic distribution of Erebus. Cross denote the seismic stations and diamond is showing the epicentral location of the highest correlation value. Lower panels show the N-S and E-W cross section. Color scale in lower section gives the reciprocal of the residual of the predicted vs. the observed delay times.

#### 5.5 Identification of tremor sources at Erebus volcano

The semblance method will be applied to locate tremor episodes recorded at Erebus in the period 2000-2003. This method was chosen, considering that it can be applied to any type of tremor events and also because it provides hypocentral solution with very small errors (section 5.3.1 and 5.3.4).

#### 5.5.1 Data preparation

Twenty six tremor events were selected for location using semblance method, based upon the same assumptions described in section 5.4. Two harmonic episodes were recorded in 2000, 5 in 2001, 6 in 2002 and 11 in 2003. Two rapid-fire episodes from 2003 were also located. Signal amplitudes were normalized by the norm of the signal vector in order to reduce the influence of amplitude variations between different stations. A spectral normalization of the signal was applied multiplying each signal spectrum by the mean spectrum of each event. Then the whole signal was spliced in small windows (10 or 20 s-long). For each window, semblance values were computed at every point of a 20x20x47 search-grid, moving each signal a delay time according to the distance between the grid point and the recording station. Each window gives a partial solution of hypocentral coordinates associated with the largest semblance value. A median of these partial solutions weighted with the corresponding partial semblance value was considered as the hypocentral location of the tremor episode. Error bars were calculated at 95% of confidence using a bootstrap algorithm that generates series of 100 partial hypocentral

locations inside a range of coordinates with +/- one standard deviation.

### 5.5.2 Distribution of epicentral locations

Parameters of the epicentral locations of 26 tremor episodes are presented in table 5.2. Figures 5.29 through 5.32 show the location of these episodes (the median value of the epicentral location of each tremor episode is marked with a red cross, and the corresponding error ellipses with the 95% of confidence are in red). Partial semblance solutions (with a black x) are classified in three coherence groups (above 66%, between 33% to 66%, and below 33% of the maximum semblance of the entire episode). Seismic stations are denoted with green diamonds. Erebus topography is represented using 500 m- spaced contour levels.

Both tremor episodes of 2000 (09/27/00 and 12/15/00) have different epicentral areas (fig. 5.29). The episode of 09/27/00 has mean of maximum semblance values at the south-western flank (Group SW), meanwhile the episode of 12/15/00 the maximum semblance is located on the caldera plateau (Group P). Median value of the partial depth solutions for both cases is inside the [2800 : 4300 m] range below the crater.
Occurrence	Num.of	Duratio	Num.of	Latitude	Longitude	Depth (m)
mm/dd/yy	stations	n (s)	windows	South	East	
HT 09/27/00	5	100	10	$77.563 \pm 0.039$	$166.876 \pm 0.183$	-46 ± 990
HT 12/15/00	5	300	30	$77.526\pm0.021$	$167.172 \pm 0.073$	-371 ± 1166
HT 01/12/01	6	200	20	$77.489 \pm 0.029$	$167.187 \pm 0.053$	-405 ± 1423
HT 02/03/01	7	240	24	$77.509\pm0.039$	$167.203 \pm 0.120$	$-2992 \pm 1586$
HT 02/07/01	7	300	15	$77.517\pm0.042$	$166.946 \pm 0.101$	$-1748 \pm 1667$
HT 02/08/01	7	1100	55	$77.522\pm0.028$	$167.199 \pm 0.086$	-2313 ± 1219
HT 02/09/01	7	500	25	$77.520\pm0.022$	$167.048 \pm 0.128$	-3708 ± 1148
HT 01/25/02	6	1500	75	$77.507\pm0.020$	$167.106 \pm 0.097$	$-1673 \pm 945$
HT 01/26/02	6	1800	90	$77.512\pm0.015$	$167.145 \pm 0.075$	$622\pm723$
HT 02/07/02	6	120	12	$77.517\pm0.023$	$167.160 \pm 0.272$	$-2050\pm3336$
HT 02/23/02	6	200	20	$77.490\pm0.072$	$167.200 \pm 0.122$	-897 ± 641
HT 03/06/02	6	80	8	$77.570\pm0.097$	$166.892 \pm 0.338$	$-3861 \pm 2411$
HT 12/24/02	7	500	25	$77.533\pm0.016$	$166.932 \pm 0.200$	$-1089 \pm 1930$
HT 01/04/03	6	2100	105	$77.528\pm0.012$	$167.243 \pm 0.065$	$-2070\pm719$
HT 01/16/03 9h	9	300	30	$77.534\pm0.028$	$167.182 \pm 0.082$	$-2260 \pm 1440$
HT 01/16/03 12h	9	900	45	$77.525\pm0.015$	$167.110 \pm 0.092$	-946 ± 1486
HT 01/30/03	9	700	35	$77.500\pm0.012$	$167.103 \pm 0.183$	$-3302\pm1656$
HT 02/02/03	10	1400	70	$77.517\pm0.008$	$167.169 \pm 0.046$	$-1529 \pm 606$
HT 02/13/03	10	1200	60	$77.522\pm0.024$	$167.065 \pm 0.094$	$-2493 \pm 1257$
HT 02/14/03	9	500	25	$77.537\pm0.019$	$167.113 \pm 0.090$	$-1492 \pm 1138$
HT 02/27/03	9	1200	60	$77.519\pm0.018$	$167.188 \pm 0.078$	$-1454 \pm 894$
HT 03/31/03	6	480	24	$77.512\pm0.024$	$167.085 \pm 0.170$	$-957 \pm 1892$
HT 04/01/03	9	600	30	$77.536\pm0.014$	$167.044 \pm 0.123$	-2897 ± 811
HT 04/12/03	9	2200	110	$77.498 \pm 0.011$	$167.190 \pm 0.055$	$155\pm825$
RF 01/18/03	9	600	30	$77.544\pm0.019$	$167.078 \pm 0.183$	-2369 ± 1493
RF 02/01/03	10	500	25	$77.497 \pm 0.029$	$166.955 \pm 0.129$	$552 \pm 2043$

Table 5.2 Parameters of hypocentral locations



Figure 5.29 Epicentral location and error ellipses at 95% of confidence of tremor episodes in 2000 (09/27/00 and 12/15/00).

Epicentral locations of tremor episodes from 2001 (Fig. 5.30) can be also classified in the previous groups. Events of 01/12/01, 02/03/01, and 02/08/01 have the epicenter close to the summit plateau or in the upper N-NE and E flanks (Group P). Error ellipses of these events cover the plateau and the upper part of the north flank. On the other hand, tremor episodes of 02/07/01 and 02/09/01 have epicenters in the upper western flank and their error ellipses cover this area (Group SW).

Tremor episodes of 01/25/02 and 01/26/02 are located on the NW upper flank, with error ellipses elongated in the NW-SE direction. These events form an epicenter group called Group NW. Locations of the episodes 02/07/02 and 02/23/02 are in the same area of group P, and events of 03/06/02 and 12/24/02 belong to Group B. See Figure 5.31.



Fig. 5.30 Epicentral location and error ellipses at 95% of confidence of tremor episodes in 2001 (Tremor episodes of 01/12/01, 02/03/01, 02/07/01, 02/08/01, and 02/09/01).



Fig. 5.31 Epicentral location and error ellipses at 95% of confidence of tremor episodes in 2002 (Tremor episodes of 01/25/02, 01/26/02, 02/07/02, 02/23/02, 03/06/02, and 12/24/02).



Fig. 5.32 part A (captions in next page)



Fig. 5.32 Part B. Epicentral location and error ellipses at 95% of confidence of tremor episodes in 2003 (Part A: tremor episodes of 01/04/03, 01/16/03, 01/16/03, 01/30/03, 02/02/03, and 02/13/03; Part B: tremor episodes of 02/14/03, 02/27/03, 03/31/03, 04/01/03, and 04/12/03).

Figure 5.32 (part A and part B) shows also that epicentral locations of 2003 can be classified in three groups: Group P containing epicenters on the summit caldera or close to the caldera on the upper north flank. Group SW with epicenters close to CON or HOO stations) on the upper west and southwest flanks. The 01/30/03 episode has the epicenter close to LEH station and can be considered as part of Group NW.

Epicenters of two rapid-fire episodes are located in different area (Fig. 5.33). The epicenter of the event of 01/18/03 is located close to Con station, on the upper southwestern flank, while the epicenter of the episode of 02/01/03 is located on the northwestern flank. Error ellipses show different orientations and no-overlapping between them, suggesting a different source location for each event.



Fig. 5.33 Epicentral location and error ellipses at 95% of confidence of Rapid-fire tremor episodes (01/18/03 and 02/01/03).

### 5.5.3 Depth Distribution of Tremor Episodes

Figure 5.34 shows the distribution of the mean values of tremor depths and the corresponding error estimations. Focal depths for 24 harmonic tremor episodes have an average of -1626 m below sea level (about 5.4 km below the crater) with a standard deviation of 1245 m. Events with high semblance have small epicenter and depth errors. Tremor episodes of 01/25/02 and 01/26/02 with maximum semblance values larger than 0.8, have depths of -1673 to 945 and 622 to 723, suggesting that they are generated at different depth levels. It is important to mention that both events were classified as Group NW, which means that the even inside a group of epicenters tremor may have different sources. Similar conclusions can be achieved if we consider the events of 02/02/03 and 04/12/03, both from the same epicentral group, both with high semblance values, and both with small error estimations.



Fig. 5.34 Depth distribution of 24 harmonic tremor episodes recorded between 2000 and 2003 at Erebus volcano. Depths were calculated using the semblance method. Squares represent the hypocentral coordinates corresponding to the median value of partial locations calculated in small time windows (10 or 20 s-long). Error bars represent the extension of the 95% confidence range calculated using a bootstrap simulation.

### 6. MODELLING OF TREMOR SOURCE

Models for generating tectonic events can be effectively explained by a single or multiple dislocations, which are driven by a coupled-shear forces mechanism; however modeling volcanic tremor episodes is a very complex problem. Difficulties arise from almost continuous signals with emergent onsets and energy confined in multiple equally spaced overtones. Several models for harmonic tremor generation have been proposed in the past, some are based on resonance of magma chamber or conduits, while others are based on excitation of elastic waves by repetitive force impulses (Hellweg, 2000). Nonharmonic tremors have been related to hydrothermal process (Kieffer, 1984; Leet, 1988; Martinelli, 1990) and also to sequences of fracture earthquakes (McNutt, 1992).

#### 6.1 Summary of existing source models

Early attempts to find a suitable mechanism of volcanic tremor were based on a self-oscillatory process of the magma chamber (Sassa (1935), Kubotera (1974), Crosson and Bame(1985), Fujita and Ida (1999)). Schick (1981) and Seidl et al (1981) started to take account of the role of transport of fluids in tremor generation. Here, I will present a summary of some of models for generating harmonic tremors based on resonance of fluid-filled conduits or oscillations caused by fluid transport.

Models based on resonance of fluid-filled cracks are characterized by narrow spectral peaks as the oscillatory response of a fluid/gas filled crack or conduit to some general forcing function (Hellweg, 2000).

6.1.1.1 Resonance by propagation of cracks.- This model was proposed by Aki et al. (1977), Aki and Koyanagi, (1981) and Chouet (1981) based upon the deep tremor observed at Kilauea volcano. According to this model, tremor is generated by the jerky extension of a chain of cracks caused by a magmatic intrusion. The cracks are connected by narrow channels that open when magma pressure reaches a critical value, facilitating the movement of fluid from one crack to the next one. Signal frequency is inversely proportional to the crack length, and signal amplitude depends on the excess pressure and the area of extension (Konstantinou and Schlindwein, 2003). Variations in the frequency content are related to the number of cracks that are vibrating at the same time, as well as to the length of the cracks (Konstantinou and Schlindwein, 2003).

6.1.1.2 Resonance by disturbance of fluid.- The harmonic resonance of a fluid-filled crack has long been proposed as the source of harmonic oscillatory behavior at many volcanoes (Chouet, 1986, 1988, 1992, 1996). This resonance is caused by a pressure disturbance in the fluid which is not accompanied by an inflow or outflow. Depending on the duration of the disturbance, the generated signals could be a long-period event or a tremor episode. The resultant wavefield depends on: a) crack geometry, b) position and

area where disturbance is applied, c) boundary conditions for the stress on the crack's surface and the fluid flow at the crack perimeter, and d) crack stiffness C, given by Eq. 6.1, and the fluid-solid impedance contrast Z, given by Eq. 6.2.

$$C = bL / \mu d \tag{6.1}$$

$$Z = \rho_s \alpha / \rho_f a \tag{6.2}$$

where *b* is the bulk modulus of fluid, *L* and *d* are the crack length and crack thickness;  $\mu$  and  $\rho_s$  are the rigidity and density of solid,  $\rho_f$  is the fluid density and  $\alpha$  and *a* are the p-wave velocity of solid and fluid, respectively.

A pressure disturbance can generate longitudinal and lateral resonance modes of a rectangular crack that are given by 2L/n and 2W/n, where n = 1,2,3,4,..., with W the crack width. The spectrum of the far-field radiated waves is dominated by sharp peaks representing the mixing of the longitudinal and lateral modes.

Resonance models have been applied to explain tremor episodes at several volcanoes. Benoit and McNutt (1997) modeled the source of harmonic tremor at Arenal volcano as resonances of a 1D vertical conduit. Long Period events recorded in Galeras volcano were related to resonance of two cracks (L: 240-360 m; W: 130-150 m; d=0.5-3.5 mm) which are connecting the degassing magma body to the surface (Gil-Cruz and Chouet, 1997). Saccorotti et al. (2001) attribute the harmonic tremor recorded on Kilauea to the resonance of a crack with a length of 20-100 m and an aperture of few

centimeters, which is filled with bubbly water.

#### 6.1.2 Models based on conduit oscillations

Flow instabilities through magmatic cracks or conduits have been invoked at several locations to model volcanic tremor where fluids move through conduits in the subsurface (Julian, 1994; Morrisey and Chouet, 1997; Julian, 2000).

6.1.2.1 Slug Flow.- The cyclic presence of slugs, defined as regions of turbulence in a pipe flow, which are separated from the other turbulent segments by portions of laminar flow, can generate pressure differences because the turbulent slug moves through the pipe at lower velocity than the laminar part (Hellweg, 2000). This process can be repeated for a long period of time (Hellweg, 2000). This model requires a narrow channel connecting two reservoirs. Channels with dimension ratios L/d larger than 50 have been observed in dikes of eroded volcanoes (Hellweg, 2000).

6.1.2.2 Constricted flow.- Julian (1994) considered a flow inside a vertically extending crack connecting an upstream and a downstream reservoir (Fig. 6.1). When the fluid flows through a constricted channel bounded by a pair of deformable elastic walls, the velocity of the fluid and pressure of the fluid over the crack walls should be compensated according to Bernoulli's theorem which states that the quantity  $(p + \rho v^2)$  must remain constant. Bernoulli's theorem explains that at large flow speeds v, the fluid pressure p in the conduit decreases and the crack walls move towards each other, constricting the flow and causing a pressure increase which forces the channel open again. The process could

repeat itself. Closing and widening the crack generate oscillations that travel elastically through the volcano.



Figure 6.1 Lumped parameter model for the generation of tremor. Viscous incompressible fluid flows in x direction through a channel of length L with imperfectly elastic walls of mass 2M, stiffness 2k, and damping constant 2A. All motions occur in the x-y plane and is independent of z. The dynamic variables are the channel thickness h(t) and the fluid flow speed v(x,t). Taken from Julian (1994).

Numerical solutions of this model based on a system of third-order ordinary differential equations can be found assuming that fluids are incompressible, at a constant density and should consist by only one phase, motions occur in one or two dimensions, and the conduit behaves elastically, while its thickness can only change as a function of time. This model considers time **t** as the independent variable, and the channel thickness, h, and the flow speed, v, as dependent variables (Julian, 2000). Considered as a control

parameter, the pressure driving the fluid flow through the channel,  $p_1$ , the solutions show various kinds of behavior (Fig. 6.2). For small  $p_1$ , the flow is steady and no vibration occurs. At a critical pressure value, short-duration vibrations appear, resembling lowfrequency earthquakes. Increasing  $p_1$ , vibrations are continuous due to a long sequence of increase and decrease conduit thickness. Finally, at high values of  $p_1$ , a chaotic vibration is reached as a result of a period-doubling cascade (Fig. 6.3).



Fig. 6.2 Synthetic tremor series (channel thickness h versus time) showing types of behavior that occurs for different values of driven pressures p1 (from 13 Mpa to 19 Mpa). First time series: simple limit cycle. Second time series: limit cycle with one subharmonic (period two). Third time series: limit cycle with two subharmonics (period four). Fourth time series: chaotic bands (noisy limit cicle). Fifth time series: chaos. Taken from Julian (1994).



Fig 6.3 Spectra of the synthetic tremor shown in figure 6.2, computed for time series 200 s long, using Welch method of averaging periodograms. Taken from Julian, 1994.

In summary, this model offers a single explanation for different characteristics of volcanic tremors such as episodes with harmonic and chaotic behavior, systematic changes in tremor amplitude as channel geometry evolves, spectra with period-doubling effect, and frequency variations as function of amplitude.

## 6.2 Characteristics of tremor at Erebus

Tremor models must explain amplitude range, duration, spectral content and spectral variations and location of the tremor source at Erebus.

Tremor episodes cover a large range of amplitudes. Largest tremor signal recorded at SBA (37.96 km from the crater), reached 1.227  $\mu$ m on Jul. 4, 2003. The second term of the relationship given by Aki and Richards (1980) between the displacement wavefield for body waves and a point force in the *j*<sub>th</sub> direction, could give a fair approximation of the magnitude of the excitation force of tremor if it is assumed that the medium is elastic and there is neither scattering or absorption (Hellweg, 2000). In this calculation the directional cosines have their largest values ( $\gamma_i$ ,  $\gamma_j = 1$ ), a mean basalt density  $\rho$ = 3000 kg/m<sup>3</sup> (Jakosky, 1950), and the wavefield velocity is v<sub>p</sub> = 4070 m/s.

$$u(t)_{i} = (1 / 4 \pi \rho v_{p}^{2}) \gamma_{i}, \gamma_{j} (1/r) F_{o}(t-r/vp)$$
(6.3)

from Eq. 6.3, and using the values above and assuming a source 3.8 km beneath the crater, we get

$$F_{o}(t-r/vp)=2.94x10^{10}$$
 N.

If we consider a source with a double couple mechanism, the shear dislocation of strength M<sub>o</sub> can be estimated using the far-field displacement components given by Eq. 6.4 derived from Aki and Richards (1980):

$$u_{(t=\infty)} = M_0 (1/4\pi\rho r^2 [\frac{1}{2} (3/v_s^2 - 1/v_p^2) \sin 2\theta \cos \phi r + (1/v_s^2) (\cos 2\theta \cos \phi - \cos \theta \sin \phi \phi)]$$
  
Eq. (6.4)

assuming  $\theta$ =45° and  $\phi$ =0 for maximum p values, and the maximum displacement

$$M_0 = 2.82 \times 10^{14} \text{ Nm}$$

which using the Eq. 6.5 given by Kanamori (1977) with  $M_0$  in dyna cm.

$$M_w = 2/3 \log 10 M_o - 10.7$$
 (6.5)

is equivalent to a magnitude  $M_w$ = 3.6. These values suggest the presence of a strong tremor at Erebus.

### 6.2.2 Location

Assuming locations provided by the semblance modeling, tremor episodes at Erebus have a deep source (~5.4 km) located beneath the crater. This source location is in agreement with the fact that tremor activity is not accompanied by surface manifestations of activity. Linear regressions of GPS data collected on 2001, showed horizontal deformations of 0.1 mm/year for CON-NKB and CON-E1S baselines (Kyle et al., 2001). Based on GPS data Bartel et al. (2003) found consistent small horizontal motions in a 3-year period which are consistent with a small volume perturbation around 5 km depth. At this depth, a basaltic magma with a hydrostatic pressure of 147 *MPa*, has a solubility of CO<sub>2</sub> of 0.075 % in weight and a solubility of 4% of water (Wallace and Anderson, 2000). The SO<sub>2</sub> emission rates of Erebus are extremely low compared to most

volcanoes (Zreda-Gostynska, 1997). These values suggest that only  $CO_2$  can be present as a gas free phase at that depth, and magma can be considered at that depth as a singlephase fluid. For a seismic signal generated by fluids at 5 km depth, Kumagai et al. (2003) found that the fluid in the resonator should be magma filling a dike.

### 6.2.3 Duration

Duration of tremor episodes has a mean of about 1 hour between 2000 through 2003. This strongly suggests that the mechanism of generation of tremor has a clearly non-destructive behavior or is occurring at multiple sites. The persistence of tremor for about 3 years also supports this consideration.

#### 6.2.4 Frequency content

Frequency content of tremor episodes observed in this study is consistently located in the range of 1-3 Hz (Fig. 2.14) for all stations. Very few events have the largest energy concentration at frequencies larger than 5 Hz. These results do not support a source process based on rock fracture or fault slip because rock-fracture signals should have broad spectra and high frequencies at least in the stations closest to the source. Most of the high frequency events are though to be related to shear failure or slip process (McNutt, 2000).

The majority of the tremor episodes at Erebus have at least one clear harmonic

(an amplitude peak located at multiples of the fundamental frequency  $f_0$ ). Almost 5% have 10 or more overtones. These frequency pattern cannot be explained by amplifications due to a path effect as was suggested by Gordeev (1992, 1993) and Seidl et al. (1981), because the same frequency peaks are observed at many different azimuths and distances. The gliding effect observed in about 50% of the tremor episodes can not be explained as a path effect. The gliding effect can be explaining by a variation of the resonator dimensions or by changes in excess pressure in the conduit (Neuberg and O'Gorman, 2002).

Period-doubling has been also documented on Erebus tremor episodes, with the presence of sub-multiples of spectral periods. This phenomenon can be clearly seen on the tremor episodes of July 2, 2003 (Fig. 4.11) and July 17, 2000 (Fig. 4.5).

The main spectral characteristics (low frequency range, number of harmonics, gliding effect and secondary spectral peaks) should be explained as expressions of a source process.

#### 6.2.5 Q value

Q values for several tremor episodes were calculated using the relation:

$$Q = f / \Delta f \tag{6.4}$$

where f and  $\Delta f$  are, respectively, the frequency and the width of the spectral peak at its half-energy level. Table 6.1 show some of the highest Q-values obtained from tremor

signal at Erebus volcano. Aki et al. (1977) found the following relationship for Q and the impedance contrast Z, in case of a fluid-filled spherical resonator:

Q= 
$$\pi / \ln [(Z+1)/(Z-1)]$$
 (6.5)

using this expression, we found the expected Z values for Erebus (Table 6.1).

Date	f (hz)	f2-f1	Q	Ζ
1/4/03	4.200	0.040	105	66.8
1/15/03	1.510	0.020	75.5	48.1
1/17/03	0.717	0.011	65.2	41.5
1/30/30	2.830	0.060	47.7	30.4
2/13/03	4.210	0.060	70.2	44.7
2/15/03	5.320	0.060	88.7	56.5
3/26/03	1.060	0.020	53	33.7
5/30/03	0.510	0.014	36.4	23.2

Table 6.1 Q values for tremor episodes at Erebus volcano.

However in case of a magmatic source located 5 km below the crater, we should assume a crack filled with magma (perhaps basanite, a phonolite parental magma), with a  $v_{pf}$ = 2320 m/s and a density of  $\delta_f$ = 2600 kg/m<sup>3</sup> (Dibble, 1994), and a hosting rock with  $v_{pr}$ = 4070 m/s (Dibble et al., 1994) and a rock density of 3000 kg/m<sup>3</sup>. Applying these values, values of  $Z_{rf}$  = 2.03 and Q= 2.91, were obtained. These results show an important discrepancy with the impedance contrasts obtained from the signal spectra. If we consider a fluid-filled crack, Z will also depend on the crack stiffness defined by Eq. 6.1, which introduce more variables in our model. On the other hand, Ferrazini and Aki (1987) found a very low velocity crack wave that contributed to high Q values in shallow resonance conduits.

### 6.3 Discussion of applicable models

Applicability of resonance models (jerky extension of cracks and resonance of fluid-filled conduits) has several problems in case of Erebus tremor:

- Extension of resonator.- If we consider the shortest frequency observed at Erebus tremor ( $f_0 = 0.25$  Hz), and a p-wave velocity of 2.5 km/s for andesitic magma, we may obtain a resonator with a length of 10 km, which contradicts the location of tremor sources.

- The deep location of Erebus tremor discards the possibility of a tremor mechanism based on resonance of gas in an organ-pipe structure as was suggested by Schlindwein et al.(1995).

- Number of overtones.- Although these model can explain the low frequency range and also the presence of a limited number of harmonics as the result of the excitation of higher resonance modes, however, Hellweg (2000) points out that resonance of a real, physical structure, can produce neither as many overtones nor exact frequency intervals. It requires a repetitive and non-destructive forcing mechanism driven by mass transport

or pressure fluctuations.

- Impedance contrast.- Very high Q values obtained from some tremor episodes listed on Table 6.1, imply a high impedance contrast in the resonance system, which is difficult to obtain for a magmatic-fluid and host rocks of Erebus volcano. However, CO<sub>2</sub> bubbles at these depths might contribute to decreasing the p-wave velocity of the fluid, and thus increasing the impedance contrast.

- Gliding.- Gliding is observed in 50% of the tremor episodes at Erebus (section 4.2.1.1), and in some cases gliding is so intense that frequency changes by much as 160% in about 10 min. Resonance models consider that these variations in frequency values are caused by changes in the conduit dimensions, however the magnitude and speed of frequency variations of tremor episodes of Erebus are difficult to explain by variations in conduit dimensions unless the source region is evolving rapidly.

- Transitions between harmonic to chaotic.- Seismic signals generated by resonance mechanisms should produce harmonic spectra. Coexistence between harmonic and chaotic parts in the same tremor episode would require a different source or external noise acting at the same time.

Considering the problems that resonance models face with Erebus data, we will focus our attention on oscillation models.

The model of oscillations generated by slug flow considers that the excitation force is caused by the pass of slugs of magma in a channel. In case of Erebus data, it would require fluid velocities close to 100 m/s (Hellweg, 2000) or channels thicker than 0.1 m in order to obtain a suitably large Reynolds number. Conduits are likely thick enough, however, it is difficult to have very high velocities in the magmatic system. One problem facing this model is the magnitude of the excitation force, which will be hard to be achieved by slug flows.

The Julian model (1994) seems to be the more suitable model for Erebus tremor because it explains satisfactorily some characteristics observed at Erebus:

- Harmonic signals.- Julian model (1994) shows that it not necessary to have a system with acoustic resonance to generate signals with harmonic spectra (energy concentrated on evenly separated spectral peaks). This type of spectrum can be modeled by non-linear systems based on third-order system of differential equations (Julian 1994; 2000).

- Period-doubling.- Julian (2000) points out that this phenomenon occurs only in nonlinear systems. The resultant spectrum has larger number of overtones and frequency peaks at values smaller than the real fundamental frequency. Changing a control parameter, new frequencies at half of the previous repetition frequency appear on a simple periodic oscillation. The output is still periodic but the repetition period is now half of the original. Further increase in the number of overtones can also transform an harmonic signal into a chaotic one. Some tremor episodes recorded on Erebus exhibit a period-doubling cascade effect in some Erebus signals, implying that a non-linear excitation is the responsible of the generation of tremor.

- Transitions between harmonic and chaotic behavior.- Period doubling is the most common route by which non-linear systems change from harmonic to chaotic behavior (Julian, 2000). It requires a high sequence of doublings to increase the period without limit and produce a chaotic signal. The reverse mechanism can also be applied.

Gliding frequencies.- Variation with time of spectral peaks can also be caused in a non-linear by changes in the amplitude of oscillations. Tremor episodes of Feb. 9, 2001 (Fig. 4.7) and Feb. 2, 2001 show gliding effect accompanied by a decrease in the amplitude signal (See section 4.4.1.2).

- Abrupt changes.- Rapid changes in the state of the oscillator can arise from abrupt changes in oscillator geometry. Such changes could be caused by breakup of a constriction, for example.

# 7. SEISMIC SIGNALS FROM ICEBERGS

#### 7.1 Introduction

Considering that highly energetic tremor activity recorded at Erebus from 2000 has been concurrent with the formation, drifting, and break-up of very large (10's of km in length) new icebergs in the Ross Sea, I will discuss the relationship between both phenomena using the results obtained by Talandier et al. (2002) and an analysis of amplitude ratios of tremor signals recorded by MEVO seismic stations in this context.

### 7.2 Ross Sea Icebergs

Large Antarctica icebergs are formed by ruptures of an ice shelf border. As icebergs drift off-shore, they are broken into smaller pieces, as well as melt, with time. The life span of an iceberg depends of its size and location, and can vary between months to years.

The largest iceberg noted to date in Antarctica (called B15), measuring 300 km by 40 km, calved off the Ross Sea ice shelf in March 2000, just few months before tremor activity started being recorded. The southwestern edge of this iceberg was at 77.3° S and 168° E, approximately 35 km northeast of Erebus crater. By 15 August 2000, B15B (135x 40 km) had detached from B15, and started drifting towards the center of the Ross Sea at a velocity of 4 km/day (Talandier et al., 2002). The remanent portion, called

B15A, stayed attached to the northern rim of the ice shelf (Fig. 7.1). On October 7, 2003, at 21:55, B15A broke into two pieces through a discontinuous E-W fracture (Neal Young, personal communication). The larger piece, and northern one, was called again B15A and the smaller one was called B15J (Fig. 7.2). Data from a GPS receiver installed on the iceberg (southern piece) suggest that the separation was caused by a southward displacement of southern piece by about 15 km during October 7 (Douglas MacAyeal, personal communication). By October 9, 2003 at 03:28, two pieces were clearly seen in satellite imagery. On November 28, satellite images show B15J rotating clockwise and drifting eastward along the shelf border, while B15A started to move toward the north (Fig. 7.3).



Fig. 7.1 NOAA-12 image of B15A and C16 iceberg calving off Ross Ice Shelf close to Ross Island, which is also covered by snow and ice. December 27, 2001. Taken from amrc.ssec.wisc.edu/amrc/iceberg.html.



Fig. 7.2 Image from the Shortwave Infrared MODIS instrument taken on October 09, 2003. Antarctic Meteorological Research Center of University of Wisconsin at Madison. <u>http://amrc.ssec.wisc.edu/amrc/iceberg.html</u>. North is shown by red arrow pointing to left -lower corner.



Fig. 7.3 November 28, 2003 NOOA 16 infrared image showing B15A, B15J, and C16. B15A and B15J are continuously moving apart. Taken from <u>http://amrc.ssec.wisc.edu</u>/amrc/iceberg.html

A smaller iceberg C16, located close to the NE part of Mount Bird, does not show evidence of major movements. Another iceberg, B17 calved off the shelf around 78° S between 165° to 175° W and drifted northward before colliding to B15B on the central Ross Sea around latitude 75° S.

#### 7.3 Location of hydro-acoustic signals between 2000 and 2001

Talandier et al. (2002) reported that 13 signals were recorded by T-phase hydrophone stations located on atolls and coral reefs of French Polynesia between August 15, 2000 to January 14, 2001 (Table 7.1). These signals have prominent spectral peaks in the 4-7 Hz band, and some of them presented overtones and gliding effects. A preliminary location using cross-correlation of spectrograms showed that these signals have epicenters in and around the Ross Sea (Talandier et al., 2002). Considering their location in the Ross Sea and their spectral configuration, Talandier et al. (2002) suggested these signals had a volcanic origin, but this hypothesis was discarded because source locations did not match any of the volcanic centers around the Ross Sea area. Further analysis showed that epicenters of these signals match with locations of huge icebergs which at that time were drifting on the Ross Sea (Talandier et al., 2002). Talandier et al (2002) proposed two mechanisms for generation of tremor-like signals between November and December 2000, one could be the collision between large icebergs (B15B and B17), and the second one would be linked to the friction on the sea floor.

Using a constant velocity of 6.5 km/s for propagation of p-waves throughout the basement, we calculated the travel distances and arrival times at the Erebus stations (E1S) for signals reported by Talandier et al. (2002). Considering a characteristic propagation velocity of Lg phases (3.2 km/s) traveling across the continental crust (Talandier et al., 2002), travel times to Erebus will be 53-154 s larger. Seismic signals from iceberg events likely travels at velocities corresponding to Lg waves because of strong surface excitation at the source.

Event	Date	Origin Time	Epicenter	Travel Distance	Arrival Time	Characteristics at MEVO stations
1	08/15/00	22:28:19	78.21 -168.61	590	22:29:50	Small signal at Mac
2	11/08/00	22:18:31	72.10 170.16	610	22:20:36	Signal at Hel 10 min earlier
3	11/12/00	01:13:27	75.76 -175.75	459	01:14:38	Not detected
4	11/12/00	~06:00:00	78.8 -175.80	456	~06:01:10	Tremor about 1 hour earlier
5	11/14/00	01:01:57	75.92 -175.60	455	01:03:07	Not detected
6	11/19/00	~02:30:00	75.8 -175.80	456	~02:31:10	Not detected
7	11/21/00	15:22:00	75.8 -175.80	456	15:23:10	At Hel arrives at 15:24
8	11/22/00	21:32:13	75.85 -176.28	443	21:33:21	Not detected
9	12/05/00	03:21:20	75.08 -177.75	457	03:22:30	Not detected
10	12/05/00	~20:46:00	75.10 -177.80	455	~20:47:10	Not detected
11	12/15/00	03:16:14	74.40 -178.40	495	03:17:30	Not detected
12	12/18/00	09:56:29	74.82 -178.68	458	09:57:39	Tremor at Abb at 09:59
13	01/14/01	17:36:36	67.00 141.50	1325	17:39:34	Not detected

Table 7.1 Origin time, travel distance, and expected arrival times from events identified by Talandier et al. (2002) if iceberg signals propagates as p-waves. Later than expected arrival times are observed by 11/21/00 and 12/18/00 iceberg signals.

These iceberg events were hardly seen on MEVO stations, due to the large epicentral distances and, perhaps, the intrinsic attenuation in the Erebus region. Figure 7.4 shows the hydro-acoustic signal recorded at VAH (French Polynesia) and the seismic signal recorded at VNDA (Antarctica) for the Event 7 (11/21/2000), with a tentative source at 75.8° S and 175.8° E. Figure 7.5 shows the corresponding records for HEL and MAC. A comparison between these spectrograms shows a snake-shaped peak in the 4-5 Hz band lasting for 3 minutes, and then followed by a lower frequency phase. This common aspect at different stations indicates a clear and characteristic source effect.

Event 12 (Dec. 18, 2000) has a predicted origin time at 09:56 UT, and epicenter on the Ross Sea at coordinates: 74.82° S and 178.68° E. Figure 7.6 shows the hydroacoustic record at VAH (Polynesia), and Figure 7.7 shows the corresponding seismic signals at HOO and ABB. Both signals show a sharp onset with high frequency content and a second phase 180 s later with an emergent initiation. No overtones are observed. Iceberg delays reported for 11/21/2000 and 02/18/2000 are in agreement with expected arrival times for Lg waves. The rest of the events were either too small to have clear arrival times or not detected at all.



Fig. 7.4 Spectrograms and time series recorded at VAH station (top) and at VNDA (bottom) of Event 7, Nov. 21, 2000, show an excellent correlation between the two spectra (Taken from Talandier et al., 2002).



Fig. 7.5 Seismic signals (top) and spectrograms (bottom) recorded at HEL and MAC stations between 15:21 and 15:31, Nov. 21, 2000. Signals from Event 7 (Table 7.1), with origin time at 15:22, are predicted to be arriving at Erebus stations at 15:24 (marked by vertical arrows), in case of waves with a velocity of 3.7 km/s (Lg phases). Hel record shows a weak 4-5 Hz signal lasting about 3 min (from time 200 to 380 s), similar to signals recorded at VNDA and VAH (Figures 7.3 and 7.4).



Fig. 7.6 The spectrogram of Event 12, Dec. 12, 2000; recorded on 11:12:30 UT at VAH (hydrophoene) is shown in the main frame. Lower frame shows a 600-s time series of this signal with a 2 Hz high-pass-filter. The frame at the right contains the amplitude spectrum of the high-pass filtered amplitude signal (Courtesy of E. Okal).



Fig. 7.7 Seismic signals and spectrograms at HOO and ABB, recording Event 12, (Dec. 12, 2000); which has an origin time at 09:56 UT marked by vertical arrows. Signals were band-pass filtered between 1-15 Hz.

#### 7.4 Amplitude distribution of tremor signals

*Rms* amplitudes of vertical components were computed for all tremor episodes recorded at Erebus. Signals were previously corrected for magnification and filtered in the 0.8 - 10.0 Hz band in order to prevent noise contamination (from microseismic noise and high frequency source). Using these signal corrections, it is expected that rms amplitudes may reflect a normal attenuation decay with distance for body or surface waves.

Assuming that these tremor-like signals are generated by the nearby icebergs (B15A, B5J or C16), the epicenters would be located at the closest epicenter to Erebus reported by Talandier et al., (2002) or at the southwestern corner of the B15A (before formation of B15J). Considering both epicenters, corresponding attenuation curves were calculated for body and surface waves. Figure 7.8 A shows that in case of a distant source (~45 km) amplitude ratios between stations of Erebus network are close to one. For surface waves, E1S/BOM is 0.99, and SBA/BOM is 0.97; and for body waves we have ratios of E1S/BOM = 0.98 and SBA/BOM = 0.93. Figure 7.8 B shows these ratios for a tremor episode located at the SW corner of B15A finding a E1S/BOM is 0.90 and SBA/BOM is 0.64; and for body waves we have ratios of E1S/BOM = 0.42.



Fig. 7.8 Upper panel shows normalized attenuation curves for a tremor episode generated at the coordinates 75.8° S and -175.8° E, using spatial attenuation. Lower panel shows normalized attenuation curves for a tremor with a source at the SW corner of B15A. Surface and body waves were used in these plots.

Using a data base with 158 tremor episodes recorded on Bom, the seismic station closest to both sources of iceberg activity, we calculated rms amplitude ratios E1S/BOM and MAC/BOM, as a way to discriminate if a signal is coming from an area close to the crater or from the B15A or C16 icebergs. Figure 7.9 shows two populations in the above mentioned ratios. One contains events with a ratio E1S/BOM smaller than 1.5, and a ratio MAC/BOM smaller than 1.0. This group would contain all events originated on icebergs and some tremor events with deep origin. The second population will be formed by


Fig. 7.9 Upper panel shows the ratios between the amplitudes of E1S/BOM and MAC/BOM for 158 tremor episodes recorded since 2000 up to 2003. Middle and lower panel contains occurrence histograms of these ratios.

An important feature of E1S/BOM ratios is the dependence with amplitude of tremor episode. Figure 7.10 shows that larger ratios occur when tremor episodes have larger amplitudes, or in other words large energy.

This analysis suggests that despite amplifications due to site-effects or complex variations of radiation field, there at least two different sources for tremor-like signals.

One group of tremor signals, which may be related to magmatic process of Erebus volcano, shows large energy releases and large E1S/BOM amplitude ratios. The second group, composed by a larger number of small amplitude signals and small E1S/BOM ratios, possibly has an origin related to the activity of nearby icebergs.



Fig. 7.10 Distribution of E1S/BOM amplitude ratios of tremor episodes with respect to the amplitude of the episode. Least mean squares and maximum likelihood regressions were calculated, showing that larger E1S/BOM are associated to large events.

## 8. CONCLUSIONS

From June 2000 till July 2003, 322 distinct episodes of tremor activity have been recorded in three extended periods by the Mt. Erebus Volcano Observatory seismic network. The first period of activity was characterized by episodes with short duration (mean=31 min.) and small amplitudes ( $v_{max} = 48.6 \ \mu m/s$ ,  $DR = 52.4 \text{ cm}^2$  in Feb. 03, 2001). The second period contains the largest amplitudes, reaching a maximum ground velocity of 97.8  $\mu m/s$  at 0.7 km from the crater on May 21, 2002 (with a reduced displacement of 92.6 cm<sup>2</sup>). The third period of activity lasted from January to July 2003, and had the maximum velocity ( $83.4 \ \mu m/s$ ). These signals are exceptionally energetic, some of them reaching values of  $2.9 \times 10^{10}$  N if the source is represented by a point force, or  $2.8 \times 10^{14}$  Nm ( $M_w$ >3.6) if the source mechanism is represented by a double couple.

Based on spectral characteristics these events are classified in three categories: harmonic (91%), chaotic (6%) and rapid-fire (3%). However, limits between these event types are not distinct because almost half of the harmonic episodes have also a chaotic component. Harmonic tremor episodes may exhibit one or up to 51 overtones in the signal spectrum. Harmonic components may have constant frequencies or undergo both gradual gliding that in just few minutes could reach 160% of frequency variation with respect to the initial frequency. In general, fundamental frequencies are confined to the 1-3 Hz band.

The wide distribution of fundamental frequency, amplitudes, and duration as well as the different source locations suggest that tremor at Erebus, has no a simple, steady source. Maybe we should considerer that tremor activity at Erebus is caused by different sources, each of them able to produce different waveforms based on slight variations of the same mechanism.

Four location methods were considered for locating Erebus tremors using a gridsearch of 50x50x90 points containing the lower and upper flanks of Erebus. The most simple method for locating non impulsive tremor signals, is based in the distribution of tremor amplitudes (*rms* of band-pass filtered tremor signals) and the depth estimation is based on fitting the observed amplitude ratio with amplitude ratios assuming a 1/rgeometric spreading. In general this method helps to constrain the area and depth range of the tremor source.

A method based on cross-correlation of signal envelopes offers very stable epicentral solutions, however depth solutions are usually larger than depths found by other methods. This method has also problems when the signal has a spectrum formed by narrow peaks which concentrate most of the energy.

Although the cross-correlation of spectrograms offered good solutions for locating a synthetic event, its application on real data was unstable. There were also problems when the tremor signal did not show gliding effect nor when the tremor had a chaotic behavior.

The semblance method showed some instabilities in the epicentral determination, especially in poor depth determination, however the median value of partial solutions was a very stable approach. Solutions remain in the same area even if the number of stations varied or if a different filter was applied.

Applying the semblance method on 26 tremor episodes recorded at Erebus between Sep. 2000 throughout Apr. 2003, at least three possible source regions were identified based on differences on location of the median of epicenters and orientation of error ellipses. All location data support the presence of a complex system of tremor sources beneath the crater and flanks of Erebus at several kilometers (4-7 km) depth below the summit, instead of a single source several kilometers long.

Location of sources, several kms below the summit, puts important constrains in the tremor generation models:

- no direct relation is observed between tremor and surface activity at Erebus crater. In contrast to other volcanoes with an open crater as Masaya or Kilauea that exhibit permanent degassing of lava fountaining, tremor at Erebus seems to be related to deep process.
- methods based on fluid-driven resonance of cracks need fluids with low velocities of propagation which are obtained with an increasing amount of free-volatiles in the

fluid.

• Location of tremor episodes -several kilometers beneath the crater or flanks- favors a method based on generation of oscillations due to instabilities in mass transport.

Julian general oscillator model (Julian, 1994), based on a non-linear model of generation of oscillations caused by transient disturbances in channel geometry when magma is transported through a constriction, seems to be the more suitable for Erebus tremor episodes. This model offers a general explanation for most characteristic patterns observed at Erebus:

- generation of submultiples of oscillation modes (doubling-period cascade effect)
- abrupt changes of the tremor character (between highly harmonic to chaotic) even in the same event.
- absence of high-frequency content.
- sustained character (tremor has been repeatedly produced for more than 3 years, with more than 300 episodes, some of them with durations of five hours) favors a non-destructive but self-modifying process of tremor generation

On the other hand, data recorded on seismic stations at Polynesia and Antarctica show that tremor-type signals can be originated by iceberg break-ups, collisions, or friction against the sea floor. Few of the signals presented in Talandier et al. (2002) have been recorded on Erebus stations. This fact opens the possibility that some tremor episodes may have an origin related to iceberg activity. This hypothesis is supported by the large amplitudes recorded at station BOM, located on the eastern flank, by the high energy of some episodes, and by the coincidence between the onset of the tremor activity and the history of iceberg formation since 2000. However, the bulk of tremor episodes recorded in 2000-2003 may have a volcanic origin as was demonstrated by the locations of all 26 episodes with a known location and by high E1S/BOM amplitude ratios. More data (currently being acquired using seismic and GPS stations on icebergs) will provide important future clues to constraining tremor and tremor like-signal sources from icebergs.

I have some recommendations for further work. These include:

- A detailed review of seismic records before 1999 may reveal more small tremor episodes that are not noticed in previous studies.
- A vector summation of the three components of broadband stations will help to better reconstruct energy release curves. These composed signals will allow new isoseismals curves and new seismic envelopes.
- Particle motions of tremor signals, especially around the fundamental frequency could offer an independent method for locating the source of these events and also for discovering the wave types that are forming the tremor wavefield.
- Seismic instrumentation on Erebus should be increased, especially with restoration of

seismic stations on the NNE flank (FNG), SE flank (ICE) and SW flank (SIS). These stations will cover flank areas that may have been hosting tremor epicenters and they will provide better coverage for more precise locations. These stations will be very valuable for any of the location methods described above.

• Strengthening ongoing collaboration with iceberg researchers, incorporating on-berg seismometer and GPS deployments, and other observations, will provide important clues to greatly clarify the relationship between tremor signals in the Ross Island region and iceberg activity.

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